International Council for the

# REPORT OF THE AD HOC MULTISPECIES 

ASSESSNENTP WORKING GROUP

Copenhagen, 18-22 June 1984


#### Abstract

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## 1. INTRODUCPTON

### 1.1 Participants

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| T Westgård | Norway |

The ICES Statistician, K. Hoydal, also participated in the meeting.

### 1.2 Terms of Reference

It was decided at the 71st Statutory Meeting of ICES (C.Res.1983/2:7) that an ad hoc Multispecies Assessment Working Group should be set up, which would meet at ICES headquarters from 18-22 June 1984 (after the routine Assessment Working Groups dealing with North Sea fish species have been convened), under the chairmanship of Mr J G Pope in order to:
(i) start trial runs with MSVPA models,
(ii) discuss the implication of their results of multispecies assessments in the formulation of management advice,
(iii) provide advice on possible further needs in relation to collection of stomach content data.

### 1.3 Background to the Working Group Meeting

Following the pioneering work of multispecies modelling of the North Sea by Andersen and Ursin, 1977, it became apparent that the problem of predation mortality was not a trivial one in the North Sea. This problem was further addressed in two papers to the 1979 Statutory Meeting of ICES by Helgason and Gislason, 1979, and by Pope, 1979. Both desoribe multispecies extensions of the familiar VPA techniques used by Working Groups and thus gave an approach to estimating predation mortality which was:

1. "Charmingly simple" (Ursin, 1982)
2. Which being retrospective enabled some of the problems inherent in a prospective model to be ignored (e.g., recruitment levels).

An ad hoc ICES Working Group was set up to consider the data requirements for multispecies assessment. The results of the ICES programme of stomach sampling (the 1981 Year of the Stomach) which that Working Group set up became available to the 1983 Statutory Meeting (Daan 1983, Armstrong, 1983 Mehl and Westgård 1983 and Gislason 1983).

The results caused considerable interest and led to the setting up of the present Ad hoo Working Group on Multispecies Assessments.

Clearly the immediate tasks for the Group has been to use the stomach data finalised in the report of the coordinators of the 1981 stomach sampling programme, Anon.1984, to make preliminary multispecies (VPA) (MSVPA) runs. This has been successfully achieved and the more obvious consequences of the results discussed. The results of such a large and complex undertaking are, however, necessarily provisional and a further meeting of the Ad hoc Working Group will certainly be needed next year to consolidate the advances made at this meeting and to develop means of giving long-term multispecies assessment advice.

The Ad hoc Working Group therefore recommends that it meet again at about the same time in 1985.
2. TEST RUNS WITH THE MULTISPECIES VPA (MSVPA)

### 2.1 FORTRAN Frogram

Before the Working Group meeting, a FORTRAN 77 program was developed for the VAX/11/750 computer at the Danish Institute for Fisheries and Marine Research. A listing of the program will appear in an ICES paper this year (Sparre, 1984).

The program is based on the NSVPA models of Pope (1979) and Helgason and Gislason (1979). The estimation of suitability indices are based on Sparre (1980). A description of the computational procedure is given in Sparre (1980), Appendices A, B and C. A flow chart of the MSVPA procedure is show in Figure 2.1.1. The program differs from the one described in Sparre (1980), only with respect to the time unit. The MSVPA used by the Working Group is based on quarterly data, whereas Sparre (1980) used annual data. A run with one particular set of parameters takes about 5 minutes on the VAX-computer.

### 2.2 Catch at Age Data for MSVPA

To satisfy the requirements of MSVPA it is neccessary to input quarterly catch at age data for each of the species to be considered. For most fish stocks definitive versions of these are not available. To test the program, preliminary estimates of these quarterly catch at age data had been derived in advance of the meeting from annual data available in various Working Group documents.

Quarterly catch at age data were estimated, assuming that fishing mortality does not vary appreciably between quarters within years. In the time available to it the Working Group were clearly unable to produce precise quarterly catch at age data.

More-over it was felt that the production of definitive quarterly catch at age data is the responsibility of the various species Working Groups who have the required data and experience. The Working Group therefore decided to check that the test quarterly catch at age data were broadly sensible in order that MSVPA results should not be greatly altered when the definitive data become available.

In the case of cod, haddock and whiting, the test data were found to be reasonable. Explicit quarterly data for Fngland, Denmark, Netherlands, Norway and Scotland for the period 1981-1983 were made available to the Group. The data for 1981 were worked up on a quarterly basis and the resultant age frequencies were compared with those used in the trial MSVPA muns.

For ages 1 and older in the case of haddock and whiting and for ages 2 and older in the cese of cod it was found that the age frequencies derived from the explicit data were reasonably similar to those used in the trial MSVPAs. It was apparent, however, from the explicit data that no 0-group haddock and whiting or l-group cod are caught in the first and second quarters.

Because, however, only a partial data set was available for the explicit calculation of quarterly age frequencies it was not possible to work up definitive data for all years over which MSVPA was to be run. It was therefore decided to retain the data used in the trial MSVPAs for ages 1 and older in the case of haddock and whiting and for ages 2 and older in the case of cod. For 0-group haddock and whiting and for l-group cod it was decided to partition the estimated annual catch equally between quarters III and IV.

Also for saithe, the quarterly catch data from the trial runs of MSVPA were accepted.

In the case of Norway pout and sprat, the quarterly data given in reports of the Industrial Fisheries Working Group were used.

For sandeel, Working Group reports showed No/month for years 1979 to 1983 and No/half-year for years 1974 to 1978. Catch numbers were combined to quarterly values for years 1979 to 1983. From that, a mean percentage distribution was calculated for half-year catch numbers per age:

| Age | 0 | 1 | 2 | 3 | 4 | 5 | $6+$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Q1 | 0 | 3 | 3 | 1 | 0 | 1 | 0 |
| Q2 | 100 | 97 | 97 | 99 | 100 | 99 | 100 |
| Q3 | 89 | 98 | 99 | 100 | 99 | 100 | 100 |
| Q4 | 11 | 2 | 1 | 0 | 1 | 0 | 0 |

The reported half-year catch numbers for years 1974 to 1978 were converted to No/quarter using the distribution pattern above.

For mackerel, the quarterly catch in number by age was estimated from Norwegian data by quarter for 1982 and 1983, and from Norwegian and Scottish data for 1981. For years prior to 1981, the quarterly data estimated in trial MSVPAs were used.

In the case of adult herring (2+), in 1981-1983, $80 \%$ of the catches in Divisions IVc - VIId was allocated to the 4th quarter each year, and the rest was allocated to the lst quarter. In Divisions IVa - IVb, catches were assumed to be equally divided between the 2nd and 3 rd quarters. Again for years prior to 1981, the catch data in the trial MSVPA were used. The seasonal distribution of l-group catches was estimated from Danish data from 1983, applying the same percentage distribution to earlier years. $75 \%$ of the 0-group was assumed to be caught in the 3rd quarter, and $25 \%$ in the 4th quarter.

The catch data used for the different species are given in Table 2.2.1.

The Stomach Sampling Project was limited to ICES Sub-area IV, and Sub-area IV was taken as the appropriate area for a North Sea multispecies model.

The Working Group recognised in this connection two problems. Firstly, for some stocks (e.g. mackerel), catches in Division IIIa are included in the assessment, and estimated stock sizes will, therefore, include some fish not present in the North Sea. No attempt was made to correct for this at the present meeting. Secondly, there are stocks which at certain times of the year, or during certain life stages, are partly outside the North Sea proper. One example is mackerel, which during summer and autumn is partly in Division IIa, and during winter partly in Division VIa. Another example is saithe. The youngest age groups of saithe are to a large extent distributed in Norwegian coastal waters and should therefore not be included in a North Sea multispecies model.

The problem with the saithe was considered the most serious. By including the youngest age groups one would heavily overestimate predation by saithe in the North Sea. It was therefore decided to exclude age groups $0-3$ when calculating saithe predation.

The best way of dealing with such problems as mentioned above in the future would be that the relevant Assessment Working Groups gave some guidance, trying to quantify the proportions being outside the North Sea.

Recommendation: The different Assessment Working Groups should at future meetings supply quarterly catch at age data for use in a MSVPA. They should also try to give some guidance concerning the proportions of different fish stocks included in the MSVPA which are outside the North Sea at different ages or different times of the year.

### 2.3 Relative Food Compositions

The input on the relative stomach contents in weight units by prey age group, and predator age group and quarter for cod, whiting, saithe and mackerel from the stomach sampling project 1981 were derived from Anon. (1984), Tables 5.2.1.a-d, 5.4.1.amd, 5.5.1.a-d and 7.5.3). Haddock data were not yet available in the proper format and this predator had to be excluded from the MSVPA.

Although mackerel, plaice and sole had been recorded in cod stomachs, there is evidence on the basis of the size distribution of these species in the stomachs that they represent discarded fish from the commercial fisheries and therefore they have been excluded as prey.

For cod and whiting, estimates of average prey weights at time of ingestion had also been provided by Anon. (1984), which deviated in some cases considerably from the average weights by age group in the various fish stocks.

It was realised that this discrepancy between the whole weight of fish found in predators' stomachs and the mean weight of fish of the same age in the sea might bias the results of MSVPA. To attempt to compensate for this, bias estimates of whole weight of fish in stomachs were used as additional inputs to some runs of the MSVPA. A more detailed discussion of this problem will be found in Section 2.7.

### 2.4 Estimates of Ration Used in MSVPA Runs

What was actually done. The total rations by quarter for the various predators entering the MSVPA as input were derived from the report of the Coordinators of the Stomach Sampling Project (Anon., 1984). It should be noted that in their report there is no consistency in the models used to estimate the consumption by the various fish species.

For cod and whiting the method of Daan (1973) has been applied according to a linear model of the equation:

$$
\text { Raily }^{\bar{R}}=2 \times \mathrm{S} / \mathrm{p}
$$

where $\overline{\mathrm{R}}$ representsrood consumption, $S$ average stomach contents in weight and $\rho$ the digestion time in days. For whiting a constant digestion time of 2.5 days was applied over all age groups. For cod allowance has been made for digestion time to vary with size of predator in view of the larger prey items consumed according to the equation

$$
\rho=\sigma F L^{2}
$$

Where $L$ is the mean length per age group and $\sigma$ is a digestion constant which has been estimated for cod at 0.06 by Daan (1973).

For saithe and mackerel exponential digestion models have been applied, taking into account the ambient temperature ( $T$ ). The model used for saithe has been given by Gislason (1983):

$$
\mathrm{R}=0.0266 \text { \# } \operatorname{EXP}(0.096 \ldots \mathrm{~T}) 3 \mathrm{~W}^{0.74}
$$

where $W$ represents the average weight of an age group. For mackerel a slightly different formulation is used where the ration is directly derived from the stomach content weights (Mehl and Westgård, 1983):

$$
R=0.005 \cdots \operatorname{EXP}(0.2 ¥ T) \because S
$$

Various other possible approaches
A. Some guesses

1. Estimates of ration assuming_ration proportional_to body_weight

Rations of l-2\% bodyweight per day is often found only in the summer half year. The range of ration per year could thus be from 1.8 w to $7.3 \overline{\mathrm{w}}$.
2. Estimates _of ration_based_on requirements_to be_met

Growth, spawning, metabolic losses (routine metabolism).
If the efficiency of food conversion is assumed known: range 0.1 0.5 and:
a) spawning and metabolic losses disregarded. In this case ration per year could be from 2 x growth increment to 10 x growth increment.
b) Spawning accounted for: the weight of eggs, adjusted for calorific contents, included in growth (male losses to be disregarded ?).This would give rations larger than a by $2-$ 10 times calorific content of eggs.
c) Routine metabolic losses included: the weight loss of a fasting fish; this could be established by experiments, and would add a further increment to the estimate of ration.

## B. Feeding experiments

1. One possibility would be to feed the fish so much that they grow as in nature. It should then be possible to express food consumption as a function of body-weight. The risk in this is that the fish might not behave naturally.
2. Estimate rates of digestion (or time to digest). Calculate ration from stomach contents and coefficient of digestion. There are unsolved problems: Cod on Georges Bank and in the North Sea seem to have the same growth rate and live at similar temperatures. Yet, North Sea cod has twice as much in the stomach as Georges Bank cod. Many approaches to the estimation of digestion rates have been published, ranging from linear models to expontential models to more complicated models, yet, it does not seem well known what determines the rate of digestion in a given situation.

## C. Calculation of requirements from the growth equation

Another possibility is to estimate ration from consideration of the growth equation: Consider the expression

$$
\mathrm{dw} / \mathrm{dt}=\mathrm{Hw}^{2 / 3}-\mathrm{kw}
$$

The positive term can be perceived as proportional to the ration $d R / \alpha t$. Some food is not digested and the equivalent of some is spent on energy for processes of feeding, digestion, etc. ("apparent specific dynamics action"). Thus:

$$
\begin{aligned}
& H w^{2 / 3}=v \frac{d R}{d t} \\
& \frac{d R}{d t}=\frac{H}{v} w^{2 / 3}
\end{aligned}
$$

where $H=3 \mathrm{KW}{ }^{1 / 3}$. If $90 \%$ of the food is assimilated and $15 \%$ of this covers "expenses" we have $v=0.9(1-0.15)=0.765$. As an example, take the growth parameters of cod in the North Sea as estimated by Beverton and Holt 1957:

$$
\begin{aligned}
& W_{\infty}=20000 \mathrm{~g}, \mathrm{~K}=0.2 \cdot \text { We have } \\
& \mathrm{H}=3 \times 0.2 \times 20000^{1 / 3}=16.29 \\
& \frac{d R}{d t}=\frac{H}{v} \mathrm{w}^{2 / 3}=21.3 \mathrm{w}^{2 / 3} .
\end{aligned}
$$

| $\mathrm{w}(\mathrm{g})$ | Annual cons. (g) |
| :---: | :---: |
| 10 | 99 |
| 100 | 459 |
| 1000 | 2130 |
| 10000 | 9887 |

Different sets of the four parameters of the growth equation Hw ${ }^{m}$ $\mathrm{kw}^{\mathrm{n}}$ may represent the observed growth equally well.

Consider the ratio of annual consumption to body-weight for three such parameter sets shown in the text table below:

| $w$ | $16.29 w^{2 / 3}-0.6 w$ | $30 w^{0.58}-2.0 w^{0.78}$ | $26 w^{0.69}-5.1 w^{0.84}$ |
| :---: | :---: | :---: | :---: |
| 100 | 4.6 | 5.7 | 8.2 |
| 1000 | 2.1 | 2.2 | 4.0 |
| 10000 | 1.0 | 0.8 | 2.0 |

The two right-hand columns represent attempts at finding physiologically plausible parameter values. The left-hand column is the standard growth equation with parameters as estimated above. The middle column parameters were adopted by Andersen and Ursin 1977 (cf.6.4). For comparison, the computer output presented at the beginning of the meeting produces the following values for four species:

Ratio $=$ annual consumption/body-weight

| COD |  | WHITING |  | SATMHE |  | MACKEREL |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| W | ratio | w | ratio | w | ratio | W | ratio |
| 520 | 4.2 | 100 | 2.4 | 330 | 3.9 | 200 | 4.8 |
| 13500 | 1.6 | 780 | 1.7 | 8700 | 2.1 | 680 | 2.1 |

The value for cod of 520 g is similar to that obtained with the standard growth equation. The value for large cod compares better to the righthand column of the previous table, whose parameters were estimated from metabolic rates of fed and fasting cod in aquaria. The parameters of the other two columns were estimated from field data on size-at-age. Generally, the consumptions calculated by the Stomach Group are in fair agreement with the more theoretical approach. It does not seem likely that the actual food consumption can have been less than half the values estimated by the Stomach Group. Such halved values would give the lower range of believable values.

### 2.5 MI Levels Used in Runs

The MSVPA model partitions natural mortality into two components.
M $1=$ "other cause" natural mortality
M 2 = natural mortality caused by predation by species included in the MSVPA

Some sources of MI mortality are:

1. Diseases
2. Physiologically-based mortality (higher metabolic rates giving high mortality)
3. Spawing strain
4. Senility
5. Starvation
6. Emigration (immigration: negative MI)
7. Predation by species not included in the MSVPA

Traditionally, we assume sources of mortality independent of each other ( $F+M=Z$ ). The possibility that a fish is caught because it was dying from "natural" causes is disregarded. The problem may be more important when it comes to separate M1 and M2 putting M1 + M2 = M. R Jones (1982) suggests that fish consumed are "displaced" specimens, weaker than others. Predation mortality might therefore be overestimated when all fish in the stomach are assumed to be viable in the absence of predation. Some may have been eaten because they were damaged (even killed) by fishing gear. The choice of MI is thus a difficult one.

At the present stage of multispecies modelling it seems advisable not to diverge from assumptions made by the Assessment Working Groups unless species interactions clearly indicate changes. Therefore, the natural mortality of large fish which are not preyed upon should be close to the constant M adopted by the Assessment Working Groups. For old age groups of smaller species on which there is still some predation, MI should be chosen such that M1 + M2 approximately equal the M of the Assessment Working Groups.

One precaution seems pertinent: in order not to overestimate predator stocks, M1 for these should perhaps be chosen smaller than tradition indicates.

The text table below shows:
A. MI values used to produce preliminary test in the computer output available at the beginning of the meeting.
B. M2 as an average for the two oldest age groups in the same output
C. $M 1+M 2=M,(A+B)$
D. M as adopted by recent Assessment Working Groups

| Species | Natural Mortalities |  |  | Working Group |
| :---: | :---: | :---: | :---: | :---: |
|  | M1 | M2 | M | M |
|  | A | B | C | D |
| Cod | 0.1 | 0 | 0.1 | 0.2 |
| Haddock | 0.1 | 0 | 0.1 | 0.2 |
| Whiting | 0.1 | 0 | 0.1 | 0.2 |
| Saithe | 0.1 | 0 | 0.1 | 0.2 |
| Sprat | 0.2 | 0.76 | 0.96 | 0.8 |
| Norway pout | 0.2 | 0.62 | 0.82 | 1.6 |
| Sandeels | 0.2 | 0.60 | 0.80 | 0.5 |
| Mackerel | 0.08 | 0 | 0.08 | 0.15 |
| Herring | 0.024 | 0 | 0.024 | 0.1 |

Thus, estimates of M for old age groups should approximate the values in column D. The values of MI finally used in the MSVPA runs are shown in Table 2.5.1. In one run these were halved to investigate the effect of the assumed value of MI.

## C. Theoretical Approaches

Jones and Johnston (1977) and Myers and Doyle (1983) relate adult mortality to spawning strategies. These papers are of similar importance to single species and multi-species assessment and seem to provide improved estimates of M for mature fish. It seems appropriate to leave the possible applim cation of such methods to the Assessment Working Groups, who should be best able to estimate sensible levels of total $M$ on older ages.
2. 6 Feeding Models Used in MSVPA and Assumptions about External Food

The MSVPA programe works with three models of feeding, The models are of Pope (1979), Helgason and Gislason (1979) and Sparre (1980). They differ mainly in the way external food is treated.

Pope (1979) explicitly ignores external food but assumes that a certain fraction of the total food consumed by a given fish is obtained from external source. Thus, it can be said that external or other food is directly proportional to the food supply consisting of fish within the model. So if a certain prey stock increases so does also the external biomass.

In Sparre's model (1980), he assumes the total biomass in the corresponding ecosystem to be constant. Thus, an increase in the biomass of fish included in the system results in a corresponding decrease of other external biomass.

The treatment of other biomass in Helgason and Gislason (1979) can be regarded as a compromise since they basically assume external food to be constant independent of the biomass of fish.

### 2.7 Problems With the Choice of Appropriate Mean Weights at Age for Prey

 Items in MSVPABackground. Results of the MSVPA are doubtlessly sensitive to the mean stock weights at age used in the analysis. Underestimates of weights will result in a larger number of individuals being eaten from a cohort and vice versa. Preliminary analyses of the stomach contents data bases (Anon., 1984) indicate that mean weights at age of prey in the stomachs of cod and whiting were, in some cases, significantly different from the assumed mean stock weights at age. These discrepancies were often substantial
(mean prey weights at age in cod stomachs ranged from 0.01 to 15 times the assumed stock weights at age for those prey items; whiting prey weights in stomachs ranged from 0.01 to 6 times the assumed stock weights). Thus, there is a potential for bias in MSVPA estimates of predation mortality unless some adjustments are made to the MSVPA model to deal with the differences in prey weights found in stomachs and in the sea. Two approaches were proposed, and it was not possible in the course of the meeting to resolve which was the more proper adjustment to the MSVPA model. The two methods of adjustment suggested involved:

1) Adjusting the suitability index for weight differences
2) Directiy adjusting M2 estimates for weight differences. These are described in Section 6.8.

In practice only the former method was investigated on an MSVPA run. An attempt to run the second method failed due to lack of convergence of the MSVPA when using this option. In the circumstances therefore all other runs were made using unadjusted stock weights for prey. Clearly further work is required on this problem.

It was pointed out that regardless of observed differences in mean-weight-at-age in the catch and in the stomachs it would be consistent to stick to the same weights-at-age throughout the models. Indeed one point of view was that what really matters is the balances of biomasses. Natural mortality (including predation mortality) is used to describe the disappearance of biomass which otherwise could be fished. On the other hand, a standardisation of mean-weight-at-age might introduce a bias in the observed growth rate of fish. The ultimate cure to these problems might ultimately be to base the MSVPA on length and age classes.

Studies of the Relationship of the Discrepancy Between Prey. Weight in the Stomach and in the Sea, to Other Factors

The second approach to adjusting for the bias suggested that the logarithm of the adjustment factor AF might be linearly related to the logarithm of the ratios of predator to prey weight in the sea. This proved a useful starting point for a more detailed study of the discrepancies between weight of prey in the stomach and weight of prey in the sea.

This relationship between the ratio of weight of the predator to the assumed mean prey stock weights and the ratio of prey weight in stomachs to prey stock weights are illustrated in Figures 2.7 .1 and 2.7.2, where:

$$
\begin{aligned}
& \text { Ratio }=\ln \left(\frac{\text { predator }}{\text { prey }}(\text { stock })\right) \\
& \text { Shatiotack }
\end{aligned}
$$

Prey species of cod exhibiting AF values greater than 0 (and thus ratios of prey weights in stomachs to those in the stook greater than one) were primarily some age groups of sprat, sandeel, herring; and Norway pout. Conversely, AF values for cod eating cod, haddock, and whiting were generally less than 0. Prey species of whiting exhibiting AF values greater than 0 were primarily sprat and sandeel, with virtually all other prey items giving negative AF values.

The differences in mean prey weights in the stomachs from the assumed mean prey weights can potentially arise from two circumstances:

1. the assumed stock weights-at-age of the prey are in error;
2. the predator species selects only a portion of the size range of the prey available.

It is quite possible, particularly for the industrial species, and for young age groups of all species, that the assumed mean stock weights may not be representative of the population. Generally, these species/age groups are minimally sampled, and the timing of these samples during the quarter may be critical since growth rates may be quite rapid.

If the size distribution of prey items is roughly equal to the optimum prey size distribution of a predator, then the values of AF should be centered at 0 with some negative and positive values. As can be seen in Figures 2.7.1 and 2.7.2, some extremely low AF values are apparent, particularly for the larger prey items (egg., cod, haddock, whiting). These data imply that only the lower portion of the size distribution of these prey items is suitable as prey.

Further analysis was undertaken to define those variables likely to influence the log-ratio of prey weights estimated from stomach contents data to prey stock weights (defined as AF). Prey weights are utilized in the MSVPA program by predator type, prey type, predator age, prey age, and calendar quarter. Some prey species were considered: cod, haddock, whiting, Norway pout, herring, sprat, and sandeels. Overall ANOVAs were conducted with AF as the dependent variable and prey type, and quarter as the categorical variables. The log-ratio of predator weight to prey stock weight was taken as a covariate in the ANOVA to remove the effects of scale. Separate analyses were conducted for the two predator species (cod, whiting) for which data were available. Results of the two overall ANOVA analyses are presented in Tables 2.7 .1 and 2.7.2.

These analyses generally indicated significant prey species, quarter, and interaction (prey/quarter) effects. Most of the variation in the ratio was explained by prey species, followed by the prey/quarter interaction. The significance of the prey/quarter interaction implies relatively rapid growth ratios of prey and thus changing size selection by predators during the year. The main
quarter effect was significant in both ANOVA analyses, but explained relatively little of the total variability. The ratio covariate was significant for the cod analysis, but non-significant in the whiting case.

Thus correction factors for differences between prey weights observed in stomachs and those in the stock should be calculated for all prey types, quarters, and interactions. The Working Group did not analyse age effects for predators or prey. Continued research on the analyses of these data are suggested.

### 2.8 The Key Run of the MSVPA

A number of runs of the MSVPA were needed in order to test the effects of various of the assumptions made. Since the MSVPA generates considerable amounts of output it was decided to provide detailed output for one key mun and to make all other runs differing from this on the various assumptions taken one at a time. The results from these could then be described by simple comparisons with the key run.

The "key run" adopted for purposes of comparison was based on

- the Helgason-Gislason feeding relationship
- the consumption figures as estimated by the coordinators of the stomach sampling programme
- residual natural mortalities to fit the standard Working Group assumptions on the oldest ages
- no correction for the difference between weights of prey in stomachs and in the stock.

Some of the central results from the key run are presented for the species considered (cod, whiting, saithe, mackerel, haddock, herring, sprat, Norway pout and sandeels) in Table 2.8 .1 which give the multispecies equivalents of conventional VPA tables, i.e., fishing mortality, population numbers, and predation mortality (total due to all predators considered). (NB. These do not include MI).

As further discussed in Section 3.1, the results do not contain any major surprises. The levels of fishing mortality are very close indeed to those obtained by the single-species Working Groups. There are substantial predation mortalities on younger age groups, mostly in the range 0 to 1 , and the numbers-at-age of the youngest age groups, estimated year class strengths, and stock biomass estimates are therefore higher than the traditional estimates by factors of up to 2 or thereabouts. These factors are not, how= ever, very variable for a particular stock.

The average fishing mortality, predation mortality and number in the stock at age for each stock are given in Table 2.9.1. (a comparison of different MSVPA runs), and these are plotted together with the estimates made by the most recent Working Group in Figures 2.8.1(a)-(j). The close agreement is clearly apparent.

The discrepancies for fishing mortality on the older ages in Figures 2.8.1.f, $g, h$ and $j$ are very probably due to different assumptions concerming terminal mortality, since the MSVPA was not "tuned" in any way.

Note that in these runs the predation mortality on saithe and mackerel has not been estimated, because of the difficulties discussed above conceming their distributions outside the North Sea, and the zero estimates should therefore be disregarded.

### 2.9 Comparing Runs Under Different Assumptions With the Key Run

Additional to the key run, time permitted a number of other runs to be made. In each of these one of the assumptions was changed. The runs are specified in the text table below:

1. Key run. No adjustment factor. Helgason-Gislason "Other Food" model M1 as in Assessment Working Groups Feeding level $=1$
2. As 1 , but feeding level $=0.5$ for all predators
3. As l, but total biomass assumed constant (Sparre, 1980).
4. As I, but ignoring other food (Pope, 1979).
5. As 1, but MI halved
6. As 1, but with stomach/stock weight adjustment factor based on suitability (See Sectiors 2.7 and 6.8.).
7. As l, but with stomach/stock weight adjustment factor based on M2. (See Sections 2.7 and 6.8). This run did not converge.

A comparison of the results of the different runs is given by species. The 1978-1983 average for F, N and M2 by age were calculated for each run and these averages are summarised in Table 2.9.1.

In order to make it possible to make a more easy comparison between the runs, the averages over years again were averaged over the age groups where predation mortality is important. The runs were then compared to the key run by expressing year-age averages as percentages of the estimates from the key runs. The percentages are given in Table 2.9.2.

Some preliminary conclusions can be made at this stage although the results are preliminary and a careful checking of the outcome was not possible during the meeting. These were:

1. The effect of halving the feeding level are higher estimates of $F$ and lower estimates of $N$ and M2
2. Ignoring "Other Food" (run 4) assumption in all cases give higher estimates of $N$ and M2 in several cases 2 times the key run value. The largest differences seem to stem from the 0-group estimates
3. Assuming total biomass to be constant (run 3) does not make any change.
4. Halving MI mainly affects $F$ and hence estimates of $N$. For sandeel and Norway pout there are, however, major changes in all three estimates
5. Adjusting for differences between the mean-weight-at-age in the stomachs and in the sea with a suitability adjustment factor gave changes in the estimates without any pattern
6. It was not possible, during the meeting, to get any runs of the Multispecies VPA using the M2 adjustment factor.

It is interesting to note that the MSVPA responds to the changes in assumptions in a predictable and stable way. Only the use of adjustment factors seemed to cause problems.

### 2.10 Preliminary Advice for Single Species Assessment Working Groups

Results from the MSVPA are as yet preliminary and the Working Group could not therefore advocate any particular set of natural mortality estimates as being the "best" ones. It was felt that should natural mortality estimates from this work need to be used in the short-term assessments then the safest set to use would be those based on the ration $\times 0.5$ run of MSVPA (Run 2).

## 3. SONE TMPIICATIONS OF THE RESULTS OF MULTISPECIES VPA TO SHORT-THRM (TACTICAL) ASSESSMENTS

### 3.1. Introduction

The results described in Sections 2.8 and 2.9 have been examined, in order to ascertain to what extent it is necessary and possib?e to advise changes to current Working Group practices to take account of multispecies effects. This advice is best considered in two parts:-

1) Short-term tactical advice (in this section)
2) Long-term strategic advice (in Section 4).

Short-term advice particularly involves the computation of short-term catch forecasts (TAC's etc.) but might also involve interim decisions, as to the direction in which fishing mortality should change, pending long-term advice becoming available.

### 3.2. Estimation of Recruitment at Age 1 in Various Stocks

Several runs of MSVPA were obtained. It was apparent from these that the results from MSVPA may vary depending on the assumptions referred to in Sections 2.3-2.7. It was therefore decided that only the "key run" would be investigated.

Estimates of the population numbers at age 1 of cod, haddook, whiting, herring, sprat and sandeel from MSVPA were plotted against corresponding Working Group estimates and against associated IYFS indices where the latter exists. Results for saithe and mackerel were not included in this procedure since, in the MSVPA, it was assumed that these species are not subject to predation. Results for Norway pout were also excluded because the Working Group series of estimates is not yet long enough.

It was found that for cod, haddock and whiting, the MSVPA results highly correlated with the Working Group results (Figures 3.2.1-3.2.3).
For herring, sprat and sandeel, a less good but still quite strong correlation exists (Figures 3.2.4-3.2.6).

If the MSVPA results so far studied turn out in future to be acceptable, it appears that almost all of the single species' assessments have been remarkably or reasonably successful in obtaining a valid picture of the relative changes occurring in recruitment to many of the commerciallyimportant fish stocks. For this reason, it is generally found that, MSVPA
estimetes of recruitment at age 1 do not correlate better with IYFS indices than do those obtained by the single species assessments (see Figure 3.2.1-3.2.6).

It thus appears on the basis of very limited experience that assessment by MSVPA is not likely to produce better relationships beiween recruitment indices and estimates of population number at age.

### 3.3. Estimates of Predation Mortality at Age

Predation mortality results from the "key run" of MSVPA are shown in Table 2.8.1.

A summary of the range of predation mortality on the three youngest age groups on which it was generally of greatest importance is shown for various species in Table 3.3.1. The results are from the "key run" MSVPA. As well as the extreme values of M2, the table shows a statistic called "upset".

This is calculated as $\exp ([\mathrm{M} 2(\mathrm{HIGH})-\mathrm{M} 2(\mathrm{LOW})] / 2)$ and indicates the percentage change in survival that a half-range deviation would cause. Thus, in the case of 0-group haddock, the highest M2 is 1.77 and the lowest 1.24. If the lover value occurred, then the survival of fish might be increased by a factor of about 1.30 from the mid-range value, while if the higher value occurred, then the survival of fish might be decreased by a factor of $1 / 1.30=.77$ from the mid-range value.

The value of upset therefore indicates to what extent the range of M 2 values might interfere with normal. single species management approaches ti) predicting catches. Factors of less than 1.20 might perhaps be thought of as being within the noise level of catch-at-age data, but values more than this might require some adjustment of $M$ from its average level in order to make a catch prediction. Such an adjustment should properly be made on a multispecies basis but might perhaps be "fixed up" on a single species basis given the biomass at age of important predators and perhaps of their alternative prey.

### 3.4. General Considerations

The results of the MSVPA runs described above all indicate substantial predation mortalities on the younger age groups of the species considered.

The effect of these on assessment calculations is not yet fully understood, and it was not possible to carry out detailed studies in the time available. The question requires careful consideration, and might be a suitable topic for studies by the Working Group on Fish Stock Assessment.

However, it is clear that the effect depends very much on the type of calculation being performed. The Working Group is reasonably confident that the effect of increasing $M$ by a fixed amount on the younger ages (especially pre-recruits) will have little effect on the calculation of short-term catch forecasts if fishing mortalities remain close to recent levels (approximately status quo forecasts).

Conversely, increased natural mortality (especially on exploited age groups) is likely to have a substantial effect on calculations used for the evaluation of longer-term strategies and biological reference
points (such as yield per recruit calculations). However (see further discussion in Section 4), these changes are of course intimately related to the interaction of one species with another, and the Working Group considers that it would be unwise to attempt to take account of such increases of natural mortality in a single-species context, until both the levels to be used and the appropriate techniques are better understood.

The increases of natural mortality do of course increase the estimates of the actual numbers of young fish in the sea, and this will have an appreciable effect on the evaluation of the consequences of the exploitation of young fish, even in the short term. If estimates of natural mortality are required for this purpose, the Working Group considers that it would be prudent to use the estimates based on the $1 / 2$ ration (Run No.2) for the time being, since these are unlikely to be overestimates. Such results should, however, be regarded as provisional, and it must be remembered that they may be substantially revised in the near future when the methodology for allowing for the different weight of fish in stomachs compared with the stock, and the suitability of the different forms of functional feeding relationship have been settled. It should also be remembered that the estimates made include an element which is on pre-recruits (which are either too young or too small to be fished), and this should be taken into account, since the mortality on pre-recruits should be of little consequence in practice in yield per recruit calcultations (and like egg and larval mortality, are part of the recruitment process).

Finally, the estimates of year class strength from MSVPA correlate very closely with the conventional VPA estimates, and do not improve the correlation with survey estimates (such as those from the IYFS). This is disappointing, but there are still interesting correlations between survey estimates which deserve to be examined, and further investigations are required, since the present results must not be considered as other than preliminary. The same conclusion applies to the study of stockrecruitment relationships, where some clarification by inclusion of predation is still a possibility.

## 4. LONG-TERM ASSESSMENTS

### 4.1. Introduction

The effects of including inter-species predation in assessment calculations are expected to be fully expressed only in the long-term assessments. They can therefore be examined either by repeating short-term forecast calculations for many years, or by carrying out analyses of yield-perrecruit type.

However, both types of calculations are a little more difficult than in conventional, single species calculations, because the natural mortalities depend on the absolute abundances of the predators. In order to determine these, the expected level of recruitment must be specified - the simple scaling of yield proportional to recruitment (which makes yield-perrecruit such a useful quantity) no longer holds good.

Forecasting recruitment in the long term is rather difficult. There seems at present to be only two reasonably workable alternatives, that is either holding all recruitments at some mean level, or specifying all
the stock-recruitment relationships. The first is likely to be misleading, and the second to be contentious. The results of all long-term forecast calculations should therefore be interpreted with great caution. It is however most important to appreciate that the full benefit of work aimed at allowing for inter-species interactions will only be apparent in long-term assessments, where it is inextricably linked with the stock-recruitment problem.

### 4.2. Previous Attempts

There have so far been relatively few investigations aimed explicitly at exploring the long-term effects of predation.

The model of Andersen and Ursin (1977) tackles this problem and particularly when a refined stock-recruitment relationship is introduced (Ursin, C.M.1978/G:47). The approach, however, is of limited applicability until the initial slopes of stock-recruitment curves for important species become known.

Calculations of repeated forecast type have been carried out by Sparre (1980), who points out that the definition of an appropriate goal function is an essential feature of longer-term strategic assessments. He also stresses the difficulties of presenting the results of any extended exploration using such models in a comprehensible way.

An example of the part of calculation which may be carried out using the yield-per-recruit approach has been given by Shepherd (1984), and the same model has been used with more realistic assumptions on a real fishery with a powerful and economically important predatory interaction by Brander (1983).

The type of calculation described by Shepherd (1984) is of a global type, i.e., designed to fully explore a wide range of fishing mortalities in a variety of competing fisheries. Such calculations are of great interest, particularly in acquiring an understanding of the way that multispecies systems work, and the implications of the assumptions made. They are, however, probably dangerous, because for choices of fishing mortalities far from current levels they are likely to involve massive extrapolations of stock size, far outside the range of recent experience. It would therefore be wise to regard the results of such calculations outside a range of about $\pm 2 \mathrm{~dB}$ (产 a factor of 1.5) around the current position as being illustrative only.

In addition, Shepherd (1984) points out that it becomes extremely difficult to display the results of this type of calculation when more than about three distinct fisheries are considered. In the real situation in the North Sea and elsewhere, a reasonably precise description of the major fisheries will certainly require the identification of more fisheries than this.

### 4.3. Alternative Presentations

The Working Group therefore considered alternative ways of organising and presenting the results of similar calculations, allowing for only small changes of fishing mortality, but many distinct fisheries. The most promising approach was felt to be an assessment of the likely changes of yield (in all fisheries) biomass and recruitment of each species, resulting
from a small ( $10 \%$ increase or decrease) in the fishing mortality in each fishery. This would lead to $a$ small stock of tables (one for each fishery), and should be relatively manageable and comprehensible.

The program used by Shepherd was available to the Working Group, and was modified by the author to permit these calculations to be carried out. Unfortunately, it was not possible in the time available to complete $a$ working version of the program, nor to assemble the considerable amount of data necessary to describe enough recognisable fisheries to construct a worthwhile example.

A sketch of the content and layout of the results of such calculations is however, given in Tables 4.3.1-4.3.4, and it is recommended that work aimed at enabling this type of information to be provided should continue.

It was however apparent from the work done that the calculations could be carried out and the results presented without any particular difficulty, for up to about 30 distinct fisheries. If it were necessary to consider more fisheries than this, some careful organisation of the calculation might be necessary, but using suitable methods, hundreds of fisheries could be considered if required (and if the necessary data were available!!).

### 4.4. Discussion

It should be noted that the parameterisation of the feeding relationship adopted by Shepherd (1984) demands estimates of parameters not immediately available from current versions of MSVPA, and that in general formulations which are convenient for hindcasting are inoonvenient for forecasting (Ursin and Sparre, pers.comm.). It would therefore be desirable if a parameterisation of the feeding relationship could be constructed which allows a realistic treatment of "other food", yet can be expressed directly in terms of prey mortality, which is most useful for prognoses. This would permit direct transfer of parameter estimates from MSVPA to forecast calculations without intemediate re-interpretation.

There do not at present seem to be any particular advantages in using either the yield-per-recruit method, or repeated time-stepping forecasts to achieve equilibrium. Both require the stocks-recruit relationship to be specified. The YPR probably requires fewer iterations (usually less than 10), whilst the time-stepped method gives potentially useful information on the dynamics of the system (or the model), since one may observe the transient approach to equilibrium, and possibly also real instabilities and cycling behaviour.

When yield curves are calculated, it should be noted that the functional feeding relationships for fish (i.e., the mortalities exerted by predators on prey as a function of predator abundance, prey abundance (all species) and external factors) are very uncertain and will be difficult to determine. The form of the feeding model is critical for long-term assessment.

## 5. ADVICE ON FUPURE DATA COLLECTION

### 5.1. Future Stomach Sampling Programmes

The results of the 1981 stomach sampling project having been implemented in the MSVPA, it is thus a suitable time to discuss the need for similar
information in future. First of all, it is clear that the extensive data collected in 1981 have actually served the original purpose to get the MSVPA going by taking account of the interactions of the exploited fish species in terms of predation. However, it is also evident that although some confidence has been gained from the general agreement between the cod results for 1981 with earlier data (Section 6), the basis for running a MSVPA over prolonged time periods is still narrow, because the tuning of the suitability matrices relies entirely on the one-year stomach content data set.

From comparing the level of intensity of sampling reached in 1981, some major differences emerge for the various species. For cod, whiting and haddock, the original aim of collecting approximately 3000 stomachs per quarter with adequate coverage of the entire North Sea was exceeded in all instances. In contrast, for saithe and mackerel, neither the intensity nor the distribution of samples has been adequate to provide reliable figures of average consumption by age groups for the total North Sea population and samples from other years had to be added. Thus, the prerequisite of tuning relative consumption in 1981 to the specific stock sizes in 1981 had to be violated. Obviously, the need for intensive stomach sampling of these species in order to improve the estimated suitability matrices still has a high priority. However, in practice, there are considerable logistic problems both in obtaining samples and in obtaining information on the seasonal spatial distribution for these species and it will be doubtful if at present any follow-up could be expected to meet the ultimate requirements.

One of the major underlying assumptions of the MSVPA is that the suitability by prey and predator age class and quarter is constant over time. After tuning the suitability matrices for the reference year to have the estimated stomach contents corresponding to the observed stomach contents, these indices are applied to calculate the food composition over all other years. However, there are various reasons why suitability indices may vary over time, the more likely ones being that 'prey switching' may occur when mejor changes in prey abundance take place or when the measure of overlap between a predator and prey population varies from year to year. Thus, there is a strong need to test the hypothesis of constant suitability, which requires that the stomach sampling program is repeated for at least some species for which 1981 has yielded a reliable estimate of suitabilities.

Since a measure of overlap could actually be estimated outside the model on the basis of research vessel data and thus used as additional input in MSVPA for years for which no stomach content data are available, it would seem appropriate to investigate possible changes in the estimated suitability matrices for individual quarters with direct estimates of the measure of overlap. This would require that stomach sampling is repeated in the same season over several years, rather than that sampling is spread over all quarters in one specific year, particularly since useful surveys for estimating measures of overlap are confined to some seasons only. Intensive surveys are carried out annually in February (IYFS), but less internationally coordinated surveys are routinely being carried out in summer as well (England, Federal Republic of Germany and Scotland). If stomach sampling were confined to these seasons, effective use could be made of existing trawl surveys and there would be no need for additional research vessel effort. It is suggested therefore that over a period of three years, intensive stomach sampling programs are continued for both
cod and whiting because these represent the two main fish predators that can be sampled adequately. However, it should be noted that with the present quarterly basis of the MSVPA, any stomach sampling program that is set up to provide an estimate of relative stomach contents for any species and quarter can be efficiently used for tuning, as long as the requirement that it reflects the total average North Sea stock is fulfilled. Thus, the continuity in sampling is a less important factor than the coverage of the total area.

There are a number of related problems, which require further reaearch and which may affect the planning of future programs. Firstly, it has been suggested that ration may be more efficiently estimated from the means of the square root of the stomach contents than from the mean stomach contents (Pennington, 1984). In order to be able to make the necessary adjustment, information has to be collected on the frequency distribution of individual stomach content weights. This problem might be solved by analysing individual stomachs instead of grouped samples, but in view of the increased workload implied, it would seem that this problem might be more efficiently solved by collecting only a subset of all the samples on an individual basis or alternatively by creating a specific independent program.

Another problem is related to the fact that the estimated indices may reflect a real change or that they may result from sampling variance. The problem of sampling variance is dealt with in more detail in Section 6.7. One solution to this problem would be to split each sample in two fractions, which are analysed separately, so that ultimately two sets of average stomach contents will be available to estimate the inherent variances. Lastly, some revisions may be required in the sub-division of predetors and preys in size classes because in some instances the classes defined in the former project appear to be too large to be used efficiently in estimating average prey weights by age and size classes, and also in size preference studies. A further breakdown would facilitate the analysis. In addition, a separation of the observed prey in stomachs into two classes according to stage of digestion might result in more accurate reporting of sizes and number of prey as well as speed up the analysis. These aspects should be more closely investigated in the actual planning process for future work.

Lastly, it was stressed that the predator prey interaotions taken account of in the MSVPA by no means can be expected to give the final answer to multispecies assessment. Interactions during the egg and larval phase may prove to be more important in regulating year class strength, but it seems unlikely that these earlier life phases could be effectively included in the MSVPA, because of mathematical restrictions in obtaining unique solutions as indicated by Magnus and Magnusson, 1983. It was felt, however, that, particularly in view of the expected upsurge of the North Sea herring stock in the near future, further studies on predation of eggs and larvae of this species would be extremely valuable, but, as yet, the background knowledge to set up a comprehensive project to study this aspect appears to be lacking.

### 5.2. Further Research

## Food preference estimates

Apart from the most obvious future work detailed in Section 5.1, there are a number of problems which could usefully be addressed by field research.

The following would be particularly useful.

## 1. Fish as food

At present, elements of the suitability matrix are estimated empirically in the MSVPA model for each separate prey age, and predator age interaction. This creates problems with age groups poorly represented in the stomach data. For instance, the suitability of large herring becomes zero because in 1981 there were few in the North Sea and none in the stomach samples. Such problems can be overcome by estimating species-specific vulnerabilities to predation and by finding functional relations of predator size to prey size. A theory is available (Andersen, 1982). It was tentatively applied by Dekker, 1983, and by Arntz and Ursin, 1981. The model requires data on food abundance by species and size class, and corresponding stomach data. Coverage of a large area or a long time is not required. It is therefore applicable to a single effort of local sampling of stomachs with simultaneous estimates of abundances in the environment. Such work might be a useful adjunct to future stomach sampling programs.

## 2. Invertebrates as food

The "other food" compartment in the three feeding models applied in the MSVPA program remains an arbitrary and somewhat obscure quantity. Its real nature could be investigated if relative suitabilities of fish and benthos were estimated for demersal predators. This requires data on the abundance of fish and important invertebrates by size class and per unit area. Data might be obtained by trawling and benthos sampling in the same place and at the same time if catchability coefficients can be estimated. A comparison of prey in the stomachs of fish in a unit area (adjusted by digestion rate) might, with food abundance data, provide estimates of the mortality coefficients created upon the benthos stocks by fish.

Such sampling might be a part of a benthos monitoring scheme which would disclose major changes in the ratio of invertebrate predators to detritus and plankton feeding in the benthos. This relates to the conceptional background of the assumption on "other food" that this is always available. The assumption is that with increased fish predation, the invertebrate predator biomass would be reduced so that the fish could feed on, for instance, what the crabs would normally eat. This phenomenon is known from oage experiments (Amtz and Brunswig, 1976; and Reise, 1977), but remains conjectural in the field.

## Ration estimates

Digestion experiments have often been performed, also in connection with the ICES Stomach Sampling Program, yet it seems that some decisive factor in the determination of digestion rates in nature has been overlooked. The difference in digestion rates estimated for cod in the North Sea and on Georges Bank are worrying (Ursin et al, 1984). The only way open to solve this problem appears to be by digestion experiments with natural foods of different species, sizes, etc. A considerable difference in food item sizes between Georges Bank and the North Sea points to item size as a possible cause, effects of which are at present poorly described in literature.

Observations on efficiencies of food conversion for different natural foods are also needed. The difference between cod in the two areas might be at least partly described as differences in food conversion. These might even be due to physiological differences in ood stocks, although this seems perhaps far-fetched. Some clear advice on how to proceed with research on this topic needs to be given by an expert.

## 6. OTHER MATTERI'

In the course of work on the MSVPA, the Working Group raised various problems and made various analyses. These may well prove the basis of further studies by individuals in the Working Group. They are presented here to stimulate these studies.
6.1. Comparison of the 1981 Stomach Sampling Results with Earlier Data

Since for cod extensive data on stomach contents have been collected in earlier years, it is possible to make a comparison between those earlier results and the results for 1981. However, there are considerable differences in the raising procedures from primary analysis to ultimate figures of total consumption, which have to be taken into account when comparing such figures.

Table 6.1.1. presents the estimated consumption in weights of various exploited fish species for 1981 with the estimates given by Daan, 1973. The values for 1981 have been obtained by multiplying the percentage weights of the different prey by age group (Daan, 1983; Table 7) with the estimated consumption for the total year (Anon., 1984; Table 7-1-2) times the estimated average stock size in 1981 from traditional VPA (Daan, 1983; Table 9). For reasons of comparability, the effect of MSVPA on the estimates of cod stock consumption has not been taken into account.

From the Table, the estimates for individual species appear to be in the same order of magnitude, and even if ranked according to importance, the two sets appear to be very close. This suggests that the two data sets are fairly consistent and that even over a period of 10 years, no major differences in the food spectrum of a predator may occur.

Daan (1983) made a comparison between the estimated feeding coefficients from three sampling programs, and the essential values are given in Table 6.1.2. These feeding coefficients are based on regressions of log transformed stomach content weights against log transformed length of cod. Since the exponent of the underlying relationship $S=a \mathrm{Lb}$ did not deviate significantly from 3 in any of the data sets, the model has been changed to $S=\emptyset \mathrm{L} 3$, where the parameter $\emptyset$ represents an index of stomach fulness and thus can be interpreted as an index of feeding level.

The values of the feeding coefficient $\emptyset$ are very close for all the three data sets (coefficient of variation $4 \%$ ), which seems to indicate that over a prolonged period, no major changes in the rate of food intake have occurred.

### 6.2. Who Eats Who?

The standard output tables from MSVPA provide detailed information on the weights and numbers consumed of each prey age group by each predator age group during each quarter of all the years included in the VPA. A major logistic problem arose when this information had to be reduced to a tractable format. Since a more comprehensive sumary would have required additional programing, only some aspects could be explored.

Since all predation is tuned to 1981 and estimates for other years reflect extrapolations, it appeared appropriate to compare the overall predation in 1981 and 1974, being the year most remote from 1981. Table 6.2.1. summarises the total weights of the various prey stooks consumed by the four predators with the estimated stock biomasses (including 0 -group) in the two years. From this Table, it would appear that the percentage of the stocks removed by predation may easily double from one year to another. Still, the relative pressure of individual predator species is even more variable, indicating that total predation is considerably buffered by differential trends in predator stock sizes.

In order to obtain a general idea of the impact of various predator age groups on different prey age groups in any particular year, the partial predation coefficients can be calculated according to:

$$
\text { M2 }(i, a, j, b)=M 2(i, a) \neq \frac{D(i, a, j, b)}{\sum_{j b} D(i, a, j, b)}
$$

where $D(i, a, j, b)$ represents the total predation in numbers of prey $i$, age a by predator $j$, age $b$. The thas estimated partial mortalities will clearly be strongly depending on the predator stock sizes and, more interesting, division by the average number of the specified age in the predator stook should represent the chance of a prey being consumed by the average predator. It is thus analogous to a catchability coefficient.

As an example in Table 6.2.2, the estimated partial predation mortalities and the mortality coefficients relating to the individual predator are given for haddock as prey. In general, the impact appears to increase with age of predator and decrease with age of prey, but particularly for cod eating haddock, the peaks appear to shift in much the same way as can be expected from a size preference.

If predators are treated like fleet operations and the assumption is made that 'catchability' by a predator is independent of prey stock size, such estimates might provide a useful starting point for shortterm predictions of expected predation mortalities given the predator stock size. Although it is not intended that the data presented here should be used in this fashion, this approach would appear to present an interesting field for further studies.
6.3. Biological Considerations and the Problems of "Other Food" and Suitability

The three feeding models (Helgason and Gislason, Sparre, and Pope) handle the role of "other foods" in different ways. These differences
may produce important differences in predictions from the same starting data (Ursin, 1982; Section 2.6 of this Report). Biological considerations may provide some guidance for decisions, when the predictions of the feeding models differ. These considerations would be particularly important when models allow "other food" to support a substantial portion of predator populations in model runs.

To make biologically sound conclusions about the true role of other foods, we must know something about them. On biological grounds, one might expect to recognise years when predators had to rely on "other foods" as years when the predators had low growth rates. Historical data from North Sea stocks might be examined for such patterns. Interestingly, in the northwest Atlantic, examination of cod growth over several years of differing capelin abundance and cod feeding habits showed no relationship between cod growth and capelin abundance (Akenhead et al., 1982). It has also been suggested that because other foods are generally of sizes most appropriate for smaller size groups of predators, the true role of other food may appear as faster growth and/or higher survivorship of younger age groups than of older ages. However, even this relationship could be absent, because if older predators are finding few prey at a time when their younger age groups are doing relatively better, it is quite plausible that older ages increase cannibalism, and obscure the suggested differences among age groups.

Although biological thinking can suggest possible roles for other food, the examples above imply that expected relationships are not present, unconvincing, or both. Long-term studies of stomach contents do, however, demonstrate great variation in use of different prey among years (Lilly, 1984; Maurer and Bowman, 1975). To clarify the role of other foods in the multispecies system, directed research efforts will probably be required. This may be possible for the demersal species, but assessing availability of other foods for pelagic species is less possible.

Because of its role in the various feeding models, other food warranted specific consideration. However, it may be a special case of a more general concern, regarding the reality of the suitability coefficients in the model. The single parameter set "suitability" is intended to reflect behavioural aspects of predation (for example, prey-palatability), local availability of prey to predators, and larger-scale distributional overlap of predator and prey stocks (Ursin, 1982). Requiring a single parameter to do several jobs at once, presents a number of modelling difficulties, but there are, however, even more aspects of predator-prey interactions which possibly need to be represented in multispecies models, rather than fewer.

The suitability coefficients should be, and are, independent of prey abundance (as long as some predator is using each prey); and they do reflect size selectivity of both predators and prey. The size preference is based on predator and prey ages though, rather then sizes, and this had led to some modelling difficulties. For reasons of both theory of predator behaviour and practical model structure, it may be desirable to develop a size-structured model of multispecies interactions and dynamics.

Currently, the suitability coefficients do not provide for responses of predator feeding to prey abundance. There are theoretical and behavioural reasons to expect such density dependent relationships on both the increasing and decreasing phases of changes in prey abundance (Dill, 1983).

Predators appaxently stick with a previously abundant prey as it becomes rarer than alternative foods. They also may not commence feeding on a previously rare food, until that species' biomass is much higher than foods which were more common earlier. Models lacking these density dependent relationships between predators and prey, may smooth pulses in prey abundance artificially. When prey in the model begins to increase, the suitability-prey biomass product tracks that change, whereas the predator's response may be more abrupt. Likewise, predators in models may switch from a prey of decreasing abundance more quickly than actual predators do, so in real systems, prey biomasses may become more depressed than occurs in models. If additional sampling is carried out synchronously with prey biomass assessments (Section 5.1), it will be possible to look for such smoothing of prey abundance changes in model predictions when compared with observed predator behaviour.

Current models treat the entire North Sea as if it were homogeneous. Realistic future models may need to address problems of spatial overlap of predators and prey. Individual age classes of both predators and prey are knowm to school together, at least in some cases. Such age, and by inference, size separation of prey stocks especially, would accentuate the lags in predator responses to changes in prey abundance discussed earlier. Such size separation, and larger-scale geographic limitations of distributions of some species (saithe, for example) could make the use of a single suitability measure for each predatorage group, prey age group unrealistic. In this context, it would be interesting to attempt to model multispecies interactions of a spatially, much more restricted, fisheries area, where the assumption of spatial homogeneity was met more closely. For such a system, model accuracy should be greater.

### 6.4. Comparison of Predation Mortalities with Earlier Estimates

The results of the extensive exercises with the North Sea echosystem model by Andersen \& Ursin (1977) were compared with estimates from MSVPA. As an example, the estimated predation mortalities for 1976 from the two models are compared in Table 6.4.1 (all model-unpublished mun). In this comparison, it should be taken into account that both models assume very similar feeding mechanisms and total consumption rates. On the other hand, the basic information on feeding available to the Andersen and Ursin model was very limited, and the input was to a large extent based on logic inferences from the available literature, whereas the MSVPA is entirely dependent on the information collected in 1981.

Inspection of the differences between the two data sets reveals two major differences: (1) The predation mortalities on saithe and mackerel are estimated at zero value in the MSVPA, since they were not recorded as prey in 1981. This is now being interpreted as young fish of at least saithe, being almost completely outside the North Sea. (2) For older sprat, the estimates from the ecosystem model have been largely underestimated. In spite of these differences, the close agreement between both the estimated trends in mortality with age and the actual
levels, indicates that the impact of predation in both exercises is virtually the same.

### 6.5. Catchability Coefficients

Age-spacific catchability coefficients to the fishing gear of research vessel surveys have been calculated on a single species basis by the "Survivor" method (Doubleday, 1981) for the North Sea cod, haddock and whiting stocks.

The results showed that the catchability coefficients were higher on younger ages. This could result from the design of the survey or from the gear used. However, it could also be interpreted as meaning that there were more fish of these ages in the sea than estimated by single species VPA, assuming constant natural mortality rate on all age groups. Thus, one conclusion could be that $M$ on these younger age groups is higher than on older age groups. Estimates equivalent to M2 values ace given in the text-table below, calculated as $\ln \{q(i) / q(i+1)$.

|  | North Sea Cod |  | North Sea Haddock |  | North Sea Whiting |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Age | $q(i)$ | M2 <br> Equivalent | $q(i)$ | M2 <br> Equivalent | $q(i)$ | M2 <br> Equivalent |
| 1 | $1.217 \times 10^{-2}$ | 0.66 | $2.840 \times 10^{-2}$ | -0.01 | $1.840 \times 10^{-2}$ | 0.45 |
| 2 | $6.263 \times 10^{-3}$ | 0.21 | $2.876 \times 10^{-2}$ | 0.53 | $1.179 \times 10^{-2}$ | 0.44 |
| 3 | $5.091 \times 10^{-3}$ |  | $1.700 \times 10^{-2}$ |  | $7.561 \times 10^{-3}$ |  |

This suggests that to a limited extent we may be able to directly observe the high levels for predation mortality that MSVPA calculates on younger ages of fish.

### 6.6. Existence and Uniqueness of MSVPA Solutions

To run a MSVPA requires the solution of a system of non-linear equations. This is done in the available computer programs with a natural iterative approximation. Questions regarding existence, uniqueness and stability are a matter of concern to the Working Group.

The Working Group has mainly focussed on the Helgason-Gislason version of MSVPA. For that, and other reasons, the following discussion is limited to that version, although some, but not all, of the following remarks apply to the versions of Pope and of Sparre. Furthermore, the following discussion relies upon the original formulae of Helgason and Gislason (1979). The computer program developed by Sparre (1984) and used in the present study, differs in the suitability coefficients. These are assumed fixed by Helgason and Gislason, whereas Sparre derives them (in an initial phase) from observed stomach contents in the year 1981. It is most likely that the following remarks apply just as much to the Sparre program.

Dekker (1982) raised these questions but was not able to prove nor disprove uniqueness of the (Helgason-Gislason) equations when used, as in the present study of the Working Group, in retrospective mode. On the other hand, he prodused a simple example showing that existence and uniqueness are not guaranteed when the model is used for predictions, i.e., in forward mode.

Magnus and Magnusson (1983) tackle the problem from a mathematical standpoint. They make, in general, the so-called "triangular assumption", i.e., that no fish preys on a fish equal or larger than itself, or more precisely, that the cohorts can be linearily ordered in such a way that a particular fish only predates upon fish in cohorts with a lower n:xmber than the number of its own cohort. Their findings can be summarised as follows:

1. There always exists a solution. This statement is also true when the triangular assumption does not hold.
2. If there are no more than 4 cohorts in the system and the triangular assumption holds, the solution is unique.
3. If (suitable) external food is suifficiently plentiful, uniqueness is guaranteed. This is not surprising, as the MSVPA approaches traditional VPA as the quantity of other food approaches infinity. On the other hand, this observation is not very useful, since a numeric value cannot be assigned to the "sufficient" quantity of external food.
4. If certain inequalities involving the data alone are true, then uniqueness holds. Here again the triangular property is assumed. These inequalities could be verified by the computer, but a corresponding sub-routine has not yet been incorporated into the program package.
5. A set of inequalities are given that guarantee the existence of a solution to the multi-species model when used for predictions. These inequalities basically require the existence of sufficient food for the fish stocks entering the model.

It should be stressed that the mentioned conditions guarantee uniqueness if fulfilled. Nevertheless, uniqueness may hold even when none of these conditions is satisfied. Thus, it still may be true that there is a unique solution in all sensible cases. The Working Group expresses the hope that further progress will soon be made in clarifying this issue.

In order to illustrate the uniqueness property, let us consider the following example.

Two species preying on each other and having the parameters:

| $\mathrm{N}_{1}(1)$ | $=823.87$ |  | $=1.24$ |  |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{W}_{1}$ | $=10$ | $\mathrm{W}_{2}$ | $=10$ |  |
| $\mathrm{R}_{1}$ | $=10$ | $\mathrm{R}_{2}$ | $=10$ | (Food cons, ration) |
| $M 1=0$ |  |  |  |  |
| $\mathrm{G}_{1}^{1}$ | $=0$ | $\mathrm{G}^{2}$ | $=1$ | ) |
| $\mathrm{G}_{2}^{1}$ | $=1$. | $\mathrm{G}_{2}^{2}$ | $=0$ | ) Suitability coefficients |
| $\mathrm{C}_{1}$ | $=100$ | $\mathrm{C}_{2}$ | $=100$ | (catch) |
| $\mathrm{F}_{1}$ | $=5000$ | $\mathrm{F}_{2}$ | $=0$ | (external food) |

In this simple case, it is easy to derive functional relationships between the average stock size of each species $\bar{N}_{1}$ and $\bar{N}_{2}$. Let these be

$$
\begin{aligned}
& \bar{N}_{1}=f_{1}\left(\overline{\mathbb{N}}_{2}\right) \\
& \overline{\mathbb{N}}_{2}=f_{2}\left(\overline{\mathbb{N}}_{1}\right)
\end{aligned}
$$

Table 6.6.1. shows solutions for $\bar{N}_{1}$ given $\overline{\mathrm{N}}_{2}$ at $\overline{\mathrm{N}}_{2}$ given $\overline{\mathrm{N}}_{1}$, and Figure 6.6.1. shows these two curves.

The MSVPA solutions are the intersections between $f_{1}$ and $f_{2}$.
It can be demonstrated that the two curves show in the Figure intersect only at the point shown. This proves that there is only one solution to the MSVPA in this example. This cannot, however, be concluded from the conditions of Magnus and Magnusson (1983) since the triangular assumption is not satisfied. It should be pointed out that in the real data used in the main study of the Working Group, the triangular assumption is not satisfied. It is therefore of great importance to expand Magnus and Magnusson's conditions so that they apply to realworld situations.

### 6.7. Sources of Varianoe of Consumption Estimates

The Report of the ad hoc Working Group on Multispecies Assessment Model Testing (Anon., 1980) recognises the many sources of variation and systematic error that stomach content data and consumption estimates are hampered with. However, since optimal stratification and sample size were impossible to evaluate at that moment, the Group did not give any requirements of confidence limits in their recommendations to the North Sea Stomach Sampling Program, 1981. Due to other priorities, the coordinators of the Stomach Sampling Program did not pay much attention to these problems in their report (Anon, 1984), and no indication of the likely confidence limits of the results is given. Such estimates will also be extremely difficult to obtain since both random sampling
variance (e.g., introduced by individual sampling of stomachs from a trawl haul) and systematic errors of unknown size due to raising factors and uncertainties in respect of digestion models, temporarily emigration of fish out of the North Sea (ref. 2.2., page 4), etc., operate simultaneously. The likely errors of the consumption estimates will also vary between species. Cod, for instance, is probably adequately sampled by bottom trawl, while several years' work had to be applied to sample the whole population of pelagic species like saithe and mackerel.

Pennington, Bowman and Langton (1980) evaluated the variability in the weight of the stomach content of cod sampled at the east coast of the USA by trawl. The general conclusion was that the individual variance within a haul is larger than variance between season, time of day, etc. The coefficient of variation was about 1.4 for all size classes of cod. If the stomach contents were to be split into individual prey categories, the coefficient of variation would become even larger.
J. Pope (unpublished data) investigated the number of 0 -group Norway pout in the stomachs of $30-34 \mathrm{~cm}$ whiting sampled haphazardly throughout the North Sea in 1978, and obtained a coefficient of variation of l.l, being the same size range as the American cod data.

Pennington (1981) sets up formulae to estimate variance of the consumption estimates when random samples are taken from a population. He gives results for silver hake indicating a standard error of $30 \%$ of the estimated total consumption. Again, a higher value might be expected if the stomach content were split into several prey species.

The present Working Group had only the data for cod in hand and there was not sufficient time to explore these data in any detail. However, some trial runs were set-up to come to grips with the problem.

No conclusive results were obtained, but the Working Group suspects, however, that the confidence limits for the consumption estimates on any one single prey species size group has rather wide limits and that if possible a higher number of stations is required than the number taken in the 1981 project.

If a new sampling scheme is to be set-up in the North Sea, a careful stratification of sampling effort should be set-up, based on the experience derived from the total data base of the 1981 program, aiming at keeping the coefficient of variation of consumption estimates of each prey species at a reasonable level. A first step should be an analysis of the variation exhibited by the 1981 stomach content data.
6.8, Two Possible Ways of Correcting the Bias in MSVPA Results due to Systematic Differences between Weights of Prey in the Sea and in Predators' Stomachs

Section 2.7 describes the discrepancies found between the weight of some prey species in the sea and in predators' stomachs. This effect seems to be systematically related to predator size with larger predators taking larger individuals from a prey cohort and smaller predators taking smaller individuals. Two approaches were developed to deal with the resulting bias in the MSVPA, but in the time available
to the Working Group, only the former could be inserted in the program, which if either is the appropriate form of correction, has to be resolved, and it is hoped that the following expositions of the alternative approaches will stimulate further work on this subject.

## Correcting for bias by adjusting the suitability estimates

Let $\bar{W}_{\text {sea }}(s, a)$ be the mean weight of age group a of species $s$ in the sea (the population mean). Let $\bar{W}_{\text {storm }}(j, b, s, a)$ be the mean weight of prey $s$ age group a observed in the stomach of predator $j$ age group $b$.
The model presented in Stare (1980) assumes that

However, as demonstrated in Section 2.7, great deviations from assumption (1) were observed. This is likely to give biassed estimates of predation mortalities, and it was attempted to correct for that. To circumvent the bias problem, a 'correction factor' was derived as follows.

Ideally, the suitability concept $\operatorname{SUIT}(j, b, s, a)$ based on age groups should be replaced by a suitability concept based on lengths.

$$
\operatorname{SUIT}(j, b, s, a)=\sum_{I} \operatorname{SUIP}_{L}(j, b, s, a, 1) \ldots \ldots \ldots \ldots \ldots .
$$

where 1 is index of prey length group.
Let $\emptyset$ ( $s, a, 1$ ) be the relative length distribution of prey ( $s, a$ ) in the sea (lengths are used rather than weights to match the actual observations of the stomach content sampling scheme).

Thus

$$
\bar{w}_{\text {sea }}(s, a)=\sum_{l} \phi(s, a, l) w_{\text {sea }}(s, a, l) \ldots . .6 .8 .3 .
$$

where $W_{\text {sea }}(s, a, 1)$ is the weight of prey ( $s, a$ ) of length $I$ in the sea. The expected mean length of ( $s, a$ ) in the stomach of ( $j, b$ ) is

$$
\bar{w}_{\text {stom }}(j, b, s, a)=\sum_{\ell} \frac{\operatorname{sui} T_{L}(j, b, s, a, l)}{\operatorname{suit}(j, b, s, a)} \phi(s, a, l) w_{s e a}(s, a, l)
$$

(see Figure 6.8.1 and compare Equation 6.8.1).

Ideally, the formula

$$
\begin{align*}
& M 2(s, a)= \\
& \frac{1}{\bar{N}(s, a) \bar{w}_{s e a}(s, a)} \sum_{j b} \bar{N}(j, b) R(j, b) \frac{\bar{N}(s, a) \operatorname{sul}(j, b, s, a) \bar{w}_{\text {sea }}(s, a)}{\sum_{d i} \bar{N}(d, i) \operatorname{SUIT}(j, b, d, i) \bar{w}_{\text {sea }}(d, i)} \quad \text { 6.8.5. } \\
& \text { should be replaced by } M 2(s, a)= \\
& \frac{1}{\bar{N}(s, a) \bar{W}_{\text {sea }}(s, a)} \sum_{j b} \bar{N}(j, b) R(j, b) \frac{\sum_{l} \bar{N}(s, a) \text { sur } \pi_{L}(j, b, s, a, \ell) \phi(s, a, l) w_{\text {sea }}(s, a, \ell)}{\sum_{d i} \sum_{l} \bar{N}(d, i) s u T_{L}(j, b, d, i, \ell) \phi(d, i, \ell) w_{\text {sea }}(d, i, \ell)}
\end{align*}
$$

Thus, the correction factor becomes

$$
C . F=\frac{\sum_{l} \bar{N}(s, a) \operatorname{sul} T_{L}(j, b, s, a, l) \phi(s, a, l) w_{\text {sea }}(s, a, l)}{\bar{N}(s, a) \operatorname{SUIT}(j, b, s, a) \bar{W}_{\text {sea }}(s, a)} \cdots \cdots \quad 6.8 .7 .
$$

C.F. is to be applied both to the nominator and the denominator in Equation 6.8.6.

Inserting Equation 6.8.4 into Equation 6.8.7, we get

$$
\text { C.F. }=\frac{\bar{W}_{\text {stom. }}(j, b, s, a)}{\bar{W}_{\text {sea }}(s, a)}
$$

Thus, to repair for the bias, $\bar{W}_{\text {sea }}(s, a)$ in Equation 6.8 .5 should be replaced by $\bar{W}_{\text {stow }}(j, b, s, a)$.

Note that an unbiassed estimate is obtained only if the condition (Equation 6.8.4) is fulfilled.

The correction for bias is to change the SUIT-values by the correction factor.

The main reason for this particular way of repairing for bias stems from the iterative manner in which the suitability coefficients are calculated in the FORTRAN program.

The mathematical equivalence:
relative stomach content $=$

6.8.9.
6.8 .10.
mast be fulfilled to secure that the iterative process converges. To replace SUIT by SUIT x C.F. does not change/spoil the equivalence.

Another approach would be to run the iterative process and afterwards repair for bias in M2 by multiplying M2 by


This idea is developed in the next Sub-section.
Correcting for bias by adjusting the M2 estimate
A second approach to this problem studied was by specifying some theoretical function for $\varnothing$ ( $s, a, 1$ ) and

$$
\frac{\operatorname{SUIT}_{L}(j, b, s, a, 1)}{\operatorname{SUIT}(j, b, s, a)} \text { in Equation 6.8.4, and from this }
$$

derive a regression function for the data presented on prey weights in stomachs of the report of the Meeting of the Coordinators of the Stomach Sampling Project, 1981 (Anon, 1984). The success of this regression can be used as a test on the assumption that the observed differences in weight are the results of the predators having a size preference for certain prey sizes within one prey year class. On the other side, the estimated regression function can be used as a predictor for the best correction factor.

Following the lines of reasoning of Andersen (1982), it was assumed that:
a) the weight of a prey in the population within one year class has a log-normal distribution (with mean $\mu$ and variance $\boldsymbol{r}^{2}$ ).
b) the size preference of a predator has the shape of a log-normal frequency distribution (with log mean/(prey to predator weight ratio) $=\eta$, and variance $\sigma^{2}$, i.e., mean log (preferred prey $\overline{\text { weight }})=\eta+\log \left(W_{\text {pred }}\right)$.

If the fraction of a year class removed by predation is not too large, it follows that the weight of a prey in a predator stomach within one year class is log-normally distributed with mean

$$
\begin{align*}
& \text { Co } x \eta+\text { Co } x \ln W_{p r e d}-C o x \mu+\mu \quad \ldots . . . . . . . . \\
& \text { where Co }=\frac{r^{2} \times \sigma^{2}}{r^{2}+\sigma^{2}} \\
& \text { and variance Co } \times \sigma^{2}
\end{align*}
$$

Assuming that $\eta, \sigma^{2}$ and $\varphi^{2}$ are independent of prey and predator age group, the different age groups were treated as multiple observations of one and the same regression function (6.8.11).

The log of the mean weight at age given by the various Assessment Working Groups was used as an estimate of $\mu$. Taking the value for $\sigma^{2}$ estimated in Dekker (1983) for cod eating gadoids as a reasonable estimate for any prey category for any predator ( $\sigma^{2} \approx I$ ), and the estimated values of the slope of the regression lines given below, it follows that the log of the mean prey weight in the predator stomach does not deviate from the mean of the log vexy significantly. Furthermore, the intercept of the regression (6.8.11) divided by its slope, should be an estimate of $\eta$. Comparing these $\eta$-estimates (given in Tables 6.8.1 and 6.8.2) to Dekker (1983), it is obvious that some $\eta$-values estimated here are utterly wrong but the general trend is in reasonable agreement.

## 7. CONCLUSIONS AND RECOMMENDATIONS

Broad conclusions and recommendations are summarised below. To aid clarity, these are cross-referenced to the relevant report section.

## Section 1

7.1.a. The ad hoc Working Group had a successful and productive first meeting. The results detailed, however, are necessarily provisional and a further meeting of the ad hoc Working Group will certainly be needed to consolidate the advances made at this meeting and to develop means of giving long-term maltispecies assessment advice.

The ad hoc Working Group on Multispecies Assessment therefore recommends that it meet again at about the same time in 1985 .

Section_2
7.2.a. A number of the inputs to MSVPA need to be estimated more precisely than was currently possible. This may be partly achieved by further research by members of the ad hoc Working Group but specific advice on quarterly catch-at-age data and proportions of the fish stocks outside the North Sea would best be provided by the relevant Assessment Working Groups. The ad hoc Working Group therefore recommend that the various Assessment Working Groups should at future meetings supply quarterly catch-at-age data for use in a MSVPA. They should also try to give some guidance concerning the proportions of different fish stocks included in the MSVPA which are outside the North Sea at different ages and different times of the year.
7.2.b. It would also be helpful if they could advise on suitable levels at natural mortality (M1 + M2) to apply to the oldest ages of each fish stock.
7.2.c. The problem of how best to adapt MSVPA to allow for differenses in the weight of fish found in stomachs and in the sea, needs further research.
7.2.d. The results of the MSVPA runs all indicate substantial predation mortalities on the younger age groups of the species considered.

## Section 3

7.3.a. The effect of including these mortalities in assessment calculations depends very much on the calculation being carried out.
7.3.b. It is the considered opinion of the Working Group that the effect of increasing $M$ by a fixed amount on younger ages will have little effect on short-term satch forecasts if fishing mortalities remain close to current levels.
7.3.c. The effect on long-term assessments (e.g., yield-per-recruit) is likely to be substantial, but it would be unwise to consider these effects of predation mortalities in a single-species context, until both the levels to be used and the appropriate techniques are better understood.
7.3.d. Inclusion of predation mortalities increases estimates of the actual number of young fish in the sea, and will have an appreciable effect on the evaluation of the consequences of the exploitation of young fish, even in the short-term.
7.3.e. If revised estimates of natural mortality are required, it would be prudent to use the estimates based on the half ration assumption (Run No.2) for the time being, since these are unlikely to be overestimates.
7.3.f. Estimates of predation mortality may include an element which is on pre-recruits, which should (like egg and larval mortality) be of little consequence in practice, for making some types of calculation (e.g., yield per recruit).
7.3.g. Current estimates of year class strength from MSVPA do not correlate better with survey indices or clarify the stockrecruitment relationship, compared with traditional estimates. This may yet be because of imperfections in the estimates, and further investigations are required.

Section 4
7.4.2. The effects of including predation mortalities in assessment calculations are expected to be fully expressed only in the long-term.
7.4.b. Predation mortalities depend on absolute predator abundances, so that yield-per-recruit calculations alone are no longer adeqiate, and the stock-recruitment relationships become of crucial importance.
7.4.c. The form of the functional feeding relationship assumed is of great importance in long-term assessments, affecting both the stability and the validity of the results. The adequacy of current assumptions is uncertain and requires further investigation.
7.4.d. The presentation of the results of long-term assessments is not easy, particularly when many fisheries are considered, and further work is required.
7.4.e. Long-term assessments may imply fish biomasses well outside the range of recent experience. The extrapolation of present interpretations of data outside a range of $\pm 50 \%$ of the current situation should be regarded as illustrative only.
7.4.f. Exercises involving running the MSVPA for years earlier than 1974, going back to the middle $60^{\prime}$ s, would give indications of the robustness of the MSVPA model due to the great changes in North Sea fish biomass that occurred during that period.

## Section 5

7.5.a. The ad hoo Working Group recommends that future stomach sampling should be particularly for cod and whiting, and should be carried out for particular quarters in 19852 1986 and 1987 using existing research vessels' surveys for sampling purposes.
7.5.b. Studies of the variability of the 1981 sampling programne should be made.
7.5.c. Studies aimed at increasing our understanding of the suitability matrix should be made and would involve the joint sampling of stomach contents and prey (including invertebrate prey).
7.5.d. Studies need to be conducted on factors of importance to predator ration size. Expert help should be sought on this problem.

## Section 6

7.6.a. The contents of the various sub-sections of Section 6 should form the starting point for a number of studies to be conducted during the year by individuals and presented to the next meeting of the ad hoc Working Group.

## 8. ACKNOWLEDGEMMENTS

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1) In species where no quarterly data were available to the Group, the annual catches were split by inserting the quarterly fishinj mortality coefficients and the annual natural mortality coefficients given here into the appropriate equations (Sparre, 1984), i.e.

$$
\mathrm{F}_{\text {quarterly }}=0.5 \quad \mathrm{M}_{\text {year }}=0.2
$$

2) Catch in numbers by age and year. The first line is the annual catch of age groups 0 to 10. The next line contains the quarterly catches of the oldest age groxp and the fishing mortality coefficient for the last quarter (input to the MSVPA). For species and periods for which quarterly dista exist, these are given.
3) Quarterly fishing mortality coefficients for the last year.
4) Quarterly weight by age in the stock (weight at age in the catch assumed to be the same).

Please note that the lay-out is only shown for cod, but applies to all species in Table 2,2.1.

Table 2.2.1. Number of years with quarterly data.

Table 2．2．1．（Continued）

| CASLH | UE WHELIINS |  |  | 0 －ANMUAL CATCH |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.58 | 0．． 0.6 | 0.3 | 0.2 | E゙ | EALTORS TO SPLIT INTG DUAETERS |  |  |  |  |  |  |
| 57016 | 7546＇82 | 97469 | 228625 | 2804a | 4．3\％： |  |  |  |  |  |  |
| 8 | 62 | 23 | 0.25 | ！ | LAST AGE GRGUF：E（ULUEST AGE） |  |  |  |  |  |  |
| 239142 | $9564.1 \%$ | 401312 | 29453 | 5482 | 46 | 7969 | 1.16 | 1385 | 142 | YEAR |  |
| 1 | い 3 ， | － 25 －23 | 0.25 |  |  |  | 545 |  |  |  |  |
| 424539 | 476651 | $1114.1 \% 3$ | 16J154 | 76447 | $13: 1$ is | S 16 |  | 2\％ 29. |  | YEAR |  |
| 10 | 7 \％ | 2 is | 6.35 |  |  |  |  |  |  |  |  |
| 664985 | 101\％151 | 560400 | 261985 | 315401 | 18292 | 4637 | ${ }^{4} 96$ | 167 | 4 | YEAE | 77 |
| 5 | 41 43 | 230 | 0， 2 号 |  |  |  |  |  |  |  |  |
| 198582 | $41826 \%$ | 33574. | 203495 | 13.53 .36 | 7618 | $30 \%$ | ． 422 | $28 \%$ | 7 | YEAR | 78 |
| 3 | $\therefore \quad 1$ | 13 | 0.025 |  |  |  |  |  |  |  |  |
| 477685 | 619543 | 466684 | 231528 | 182302 | 25082 | 31.5 | 1150 | 194 | 15 ！ | YEAR | 79 |
| 2 | ＂ | ¢ | 0.25 |  |  |  |  |  |  |  |  |
| 332378 | 321\％ 04 | 43\％6采 | 282591 | 834193 | 38185 | 80，${ }^{\text {a }}$ | 755 | $\pm 3$ | 4．）！ | SEAR |  |
| 7 | $\because$ | 42 | 0.25 |  |  |  |  |  |  |  |  |
| 543293 | 3.54242 | 354910 | 261111 | 93013 | 21701 | 1\％2\％年 | 1．261 | 2in | 301 | TEAR | 81 |
| 26 | 1.1 | 6 3 | 0.25 |  |  |  |  |  |  |  |  |
| 104914 | ） 264612 | 13682\％ | 233520 | e2116 | 34：94 | E2F9 | 1\％12 | 363 | 58 | CEAR |  |
| 12 | 9 | $5 \quad 4$ | 425 |  |  |  |  |  |  |  |  |
| 6614\％7 | － 300540 | 15920 d | 1030\％ |  | 35360 | $-4021367$ |  | 596 | $\because 81$ | YEAE 83 |  |
| 19 | 14 | 7 5 | 6.25 |  |  |  |  |  |  |  |  |  |  |
| 965 | ．08e | ． 26 | $\cdots$ | ． 21 | － 34 | ． 26.35 |  |  |  |  |  |
|  | WHITIM |  |  |  |  | $!$ | Whath | 116 | ？日土土 | NO． | 2 |
|  |  | 11 － |  |  |  | 1 | 1．40， | it 0 not | \％bk． | सGE | AT 的等。 |
|  | 0.01 | 9．0．0． | 0．028 | Cond | \％ 2.05 |  |  |  |  |  |  |
|  | 0.063 | 30.080 | 0.100 | 6， 1.2 | 20.03 |  |  |  |  |  |  |
|  | 0.145 | $50.16 \%$ | 0.184 | $\therefore 2.210$ | 00.05 |  |  |  |  |  |  |
|  | 0.231 |  | 0.269 | 6.282 | 20.06 | －！上も | 117 WE | 26H2S | （i）WH | H17506 |  |
|  | 0.244 | 4 9，30\％ | 0． $32 \%$ | （0，355 | 50.05 | S EY | Atgf |  | Aldy |  |  |
|  | 0.383 | 30.811 | 0.450 | 8 m 840 | 06.05 |  | U kts | －What | － MOHO |  |  |
|  | 0.451 | 1． 0.461 | 0.8976 | $0.3 y \%$ | 92.25 |  |  |  |  |  |  |
|  | 0．6ta | 40.832 | 0.509 | 8.55 | $2 \quad 308$ |  |  |  |  |  |  |
|  | 0．5\％ | i5 0．59\％ | 0.614 | 2． 6 mz | \％ 0.05 |  |  |  |  |  |  |
|  | 0.06 | 3 （\％）48 | 0.91 | 0． 350 | $\because \quad 9.04$ |  |  |  |  |  |  |
|  | 1）． $8 \% 5$ | $50.91 \%$ | 9.949 | $3 \times 40$ | ） 000 |  |  |  |  |  |  |

CARCH OE SHANHE


| SAITHE |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 16 | 5 |  |  |  |
| 0.010 | 0.050 | 0.100 | 0.150 | 0.05 |
| 0.200 | 0.350 | 0．340 | 0.340 | 0.05 |
| 0.440 | 0.490 | 0.590 | 0.600 | 0.05 |
| 0.800 | 0.920 | 1．060 | 1． 230 | 0.05 |
| 1.39 | 1，56 | 1．71 | 1．88 | 0.05 |
| 2.05 | 2n22 | 2．at | 2，62 | 0．05 |
| 2.83 | 3.64 | 3.24 | 3.45 | 0.05 |
| 3.66 | 3.87 | 4.09 | 4．32 | \％ 05 |
| 4.5 | 4.78 | 5.02 | \％ 2 y | 0.05 |
| 5.45 | $5.7 \%$ | 5.94 | 6．15 | 0.05 |
| 6.56 | 6.57 | 勺，$\because 4$ | 6． 8 c | 0.06 |
| 7.01 | ${ }^{7}+15$ | 7.24 | $\cdots 28$ | 0.05 |
| $\bigcirc .32$ | $\% \mathrm{Fat}$ | $\because 8.8$ | $\because \square 8$ | O．0． |
| 7.71 | $\because 84$ | $\cdots \mathrm{OH}$ | 8． 16 | 0.05 |
| E． 2 B | B．43 | 日． 61 | 8.84 | 0.05 |
| ¢，\％＂ | 9.3 | 9.30 | 9.80 | 9.05 |

！NAME UE GV゙ETES NO． 3
！MU．OE ARE GKOUNS AGE AT MAT．
－BLDY WEDBHTS UE SADTHE
！BY AGE BROUP ARD QUAFTER
1 AHI RES NAT．MOXT



## Table 2.2.1. (Continued)



| Hallmuck |  |  |  |  |  | NAME OF BPECTES NO. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | 2 |  |  |  | , | H0. IF: AGE FR.. AGE AT MAT. |
| . 010 | . 015 | - 026 | -64 0 | . 05 |  |  |
| . 072 | .095 | . 126 | -16. | . 05 |  |  |
| . 20 | -2A | -29 | - 22 | . 05 |  |  |
| . 36 | . 40 | .44 | - 79 | . 05 |  |  |
| .54 | . 59 | . 63 | . 69 | . 05 |  | QULY WEIGHIS OE HADLDEK |
| . 74 | . 79 | .83 | . 69 | . 05 |  | GY AgE GROUP AND QUARTER |
| .94 | .99 | 1.04 | 1.09 | - 05 |  |  |
| 1.14 | 1.18 | 1.23 | 1. 29 | . 0.5 |  |  |
| 1.34 | 1.40 | 1. 51 | 1.5\% | - 05 |  |  |
| 1.63 | 1.69 | 1.76 | 1.85 | . 05 |  |  |
| 1.98 | 2.0 全 | 2.15 | 2 n 28 | -65 |  |  |
| 3.31 | $2 \times 4$. | 2.46 | 2.45 | . 05 |  |  |




| (LATCH UNKNOWN) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 与民RAJ 5 | 2 |  |  |  |
| "0006 | .001 | . 0030 | .0042 | .025 |
| . 0050 | . 0064 | . 0071 | . 0090 | . 035 |
| .0085 | $\cdots 0100$ | . 0140 | . 01.60 | $=025$ |
| . 018 | - 020 | . 025 | . 027 | . 023 |
| .02\% | . 028 | . 028 | .028 | . 025 |

## /Continued

! NO OE AGE GK. AND ALEE AT KAT.

BOHY W\&JBHTS OE SERAT
! BY AGE GKOUF ANO GUAETER

- AND RES. NAT" MOKT.

Table 2.2.1 (Continued)

/Continued

| SANDEEL CA 10 | CH Number |  |  | $!1$ | : QUAETER | L. Y Cald | Ch mata |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 775000 | 1.58000 | 1.9200 | 0 | 2800 | 0 | YEAK \%A | Q1. |  |
| 1142000 | 25063000 | 511.8000 | 1900800 | 2342000 | 295200 | 108000 | $!$ |  | 02 |
| 8950000 | 598000 | 63400 | 10000 | 11900 | 6000 | 3000 | 1 |  | 03 |
| 1106000 | 12000 | 600 | 0 | 100 | 0 | . | $!$ |  | 0 |

.0001

| 0 | 559300 | 208300 | 43500 | 0 |
| ---: | ---: | ---: | ---: | ---: |
| 100000 | 16084700 | 6733700 | 4302500 | 778000 |
| 8261000 | 542900 | 1140500 | 172000 | 245500 |
| 1021000 | 11100 | 11500 | 0 | 2500 |
| 000001 |  |  |  |  |


| 7500 | 0 | $Y E A K 75$ |
| ---: | ---: | ---: |
| 744500 | 96000 | 1 |
| 2000 | 1000 |  |
| 0 | 1 | 1 |
|  |  | 02 |
|  | 03 |  |

$\begin{array}{rrrrr}242000 & 21354800 & 15166900 & 1946300 & 1336000 \\ 5452100 & 878100 & 3417600 & 76000 & 118800\end{array}$

| 2100 | 0 | $Y E A K$ |
| ---: | ---: | ---: |
| 207900 | 88000 | 01 |
| 3000082000 | 02 |  |
|  | 03 |  |

673900
.000001
$1.7900 \quad 24400 \quad 1200$
04
.0001
$\begin{array}{rrrrr}0 & 1314200 & 236400 & 68200 & 0 \\ 3696000 & 42491800 & 7709600 & 6747800 & 1090000 \\ 1.533700 & 3063600 & 930600 & 150000 & 106900\end{array}$

| 4600 | 0 | XEAK 77 | 01 |
| ---: | :---: | ---: | ---: |
| $45 \% 200$ | 402000 | 02 |  |
| 30000 | 1.8000 |  | 03 |
| 0 | 1 |  | 04 |

.0001

| 0 | 1950000 | 578600 | 23700 | 0 |
| ---: | ---: | ---: | ---: | ---: |
| 922000 | 63017000 | 18707800 | 2342800 | 1054006 |
| 43645200 | 3700500 | 636100 | 164000 | 99000 |
| 5344800 | 75500 | 6900 | 0 | 1000 |
| 100001 |  |  |  |  |
| 0 | 25900 | 121500 |  |  |


| 2000 | 0 | YEAK 7801 |  |
| ---: | ---: | ---: | ---: |
| 188000 | 82000 |  | 02 |
| 36000 | 34000 |  | 02 |
| 0 | 1 |  | $0 A$ |


| 0 | 0 | ! | YEAR | 79 | Q1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 849000 | 362700 | $!$ |  |  | Q2 |
| 29800 | 0 | 1 |  |  | 03 |
| 0 | 1 | ! |  |  | 04 |
| 0 | 0 | ! | Y (EAR | 80 | Q]. |
| 206900 | 89400 | ! |  |  | [2\% |
| 3100 | 1100 | $!$ |  |  | 23 |
| 0 | 1. | ! |  |  | $1{ }^{4} 4$ |
| $\% 500$ | 1800 | ! | YEAR | 8. | 01 |
| 361700 | 3.29700 | ! |  |  | 02 |
| 3400 | 0 | ! |  |  | Q3 |
| 0 | 1 | ! |  |  | Q4 |


| 0 | 0 | YEAR $82 \quad$ Q1 |  |
| ---: | :---: | ---: | ---: |
| 101800 | 31300 |  | 02 |
| 3900 | 10 |  | 03 |
| 0 | 1 |  | 04 |

.000001
$18327400 \quad 22943400 \quad 4729500 \quad 1269600$
.00000

| 241400 | 58785900 | 8219600 | 3788000 | 187110 |
| ---: | ---: | ---: | ---: | ---: |
| 11459400 | 4757400 | 485900 | 340800 | 3570 |
| 0 | 0 | 0 | 0 |  |

0
955400
6633600
575200
00.000001
$\begin{array}{rrrr}7900 & 7400 & 500 & 1 \\ 7907900 & 36236600 & 1022500 & 2422 \\ 543100 & 3122000 & 531300 & 17 \\ 1 & 1 & 1 & \end{array}$ .05
.0000001 .0000001 . 0000001 . 000001

| 0 | 0 | $!$ | YEAK | 83 | Q 1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 121600 | 33900 | $!$ |  |  | Q2 |
| 100 | 100 | $!$ |  |  | Q3 |
| 1 | 1 | ! |  |  |  |

SANDEEL

| 7 | 2 |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 0.0008 | 0.0015 | 0.0022 | 0.0032 | 0.025 |
| 0.0050 | 0.0060 | 0.0080 | 0.0 .100 | 0.025 |
| 0.0110 | 0.0130 | 0.0140 | 0.0150 | 0.025 |
| 0.01 .70 | 0.0200 | 0.0220 | 0.0230 | 0.025 |
| 0.0250 | 0.0260 | 0.0270 | 0.0280 | 0.025 |
| 0.0290 | 0.0300 | 0.0310 | 0.0320 | 0.025 |
| 0.0330 | 0.0330 | 0.0330 | 0.0330 | 0.025 |

- NAME OE SPECTES NO. 9

NO OF AGE GR., AGE AT MAT.
! BOLY WETEHTS OF SARLIEES
BY ABE GROUP AND QUARTER
! ANG RES. NATE MORT.


Sispototest

Table 2.5.1 Residual natural mortality, $M$, used in MSVPA Key zun.

| SPFCIES | AGE-gr | COFFFICIENT Year |
| :--- | :---: | :---: |
| Cod | AIl | 0.2 |
| Saithe | $"$ | 0.2 |
| Maokerel | $"$ | 0.16 |
| Haddock | $"$ | 0.2 |
| Herring | $"$ | 0.1 |
| Sprat | $"$ | 0.1 |
| Norway Pout | $"$ | 1.0 |
| Sandeel |  | 0.1 |

Table 2.7.1 ANOVA of COD log-ratio prey
Weight (stomach)/Prey Weight (stock) as a function of prey type and calendar quarter. COVARTATE is the log ratio predator weight/pney weight (stock).

| Source | Sum of <br> Squares | Degree off <br> Freedom | Mean <br> Square | F | Tail <br> Prob. | Regress <br> Coefficient |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Prey Species | 53.87 | 6 | 8.98 | 24.58 | 0.00 |  |
| Quarcer | 8.17 | 3 | 2.72 | 7.45 | 0.00 |  |
| Prey/Quanter | 37.17 | 18 | 2.06 | 5.65 | 0.00 |  |
| Ist Covariate | 7.56 | 1 | 7.56 | 20.70 | 0.00 | 0.1065 |
| Error | 165.13 | 452 | 0.36 |  | 0.00 |  |

Table 2.7.2 ANOVA of WHITING log-ratio prey Weight (stomach)/Prey Weight (stook) as a function of prey type and calendar quarter. COVARIATE is the log-ratio predator weight/prey weight (stosk).

| Source | Sum of <br> Squarea | Degnee of <br> Freedom | Mean <br> Square | F | Tail <br> Prob. | Regression <br> Coefficient |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Prey Speoies | 130.92 | 6 | 21.82 | 58.78 | 0.00 |  |
| Quarter | 14.73 | 3 | 4.91 | 13.23 | 0.00 |  |
| Prey/Quarter | 89.65 | 18 | 4.98 | 13.42 | 0.00 |  |
| Ist Covariate: | 1.20 | 1 | 1.20 | 3.22 | 0.07 | -0.0630 |
| Ercor | 104.68 | 282 | 0.37 |  |  |  |

1-A value for whiting eating cod in the 3rd quarter was specified in order to specify the full design.





| STUCK NUMEERS SAITHE |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| AGE | 1974 | 1975 | 1976 | 1977 | 1978 | 1979 | 1980 | 1981 | 1982 | 1983 |
| 1 | 200495. | 196632. | 209275. | 176535. | 433729. | 262488. | 296106. | 464082. | 26487. | 596. |
| 1 | －97607． | 213275. | 160989. | 171340． | 144576. | 355107. | $21490 \%$ ． | 242431. | 376683. | 21685. |
| 2 | 224430. | 36）852． | 174335. | 131601. | 1379515. | 117256. | 289933． | 175075． | 193455. | 30\％088． |
| 3 | 135703. | 170437． | 399701. | 121945. | 96065. | 97693. | 80756. | 221516. | 127450. | 136184. |
| $\stackrel{ }{ }$ | －3022． | 56585. | 93489. | 117360. | 79554. | 52135. | 70926. | 56030. | 164334. | 83101. |
| 5 | 40965. | 31210. | 25.34. | 30365. | 49543. | 40259. | 29422. | 48155. | 38244. | 104200. |
| B | 61525. | $\because 2367$ ． | 17439. | 11725. | 13257. | 25059. | 21419. | 15460 ． | 23035. | 21744. |
| 7 | 42199. | 31913. | 12275. | 9684. | 5391. | 7450. | 14335. | 11692. | 8592. | 21235. |
| s | 13110． | ¢1bls． | 14753. | 7076. | 5077. | 3369. | 3725. | 7681. | 15090. | 5484. |
| 9 | 6033. | 10313. | 9837. | 7726. | 3186. | 3196. | 1974. | 2165. | 3352. | 4267. |
| 19 | 3619. | ：\％5t． | －479． | 5377 ． | 3211. | 1973. | 2194. | 1165. | 116E． | 1865. |
| 11 | 1725. | 2235． | 2005. | 3526. | 2700. | 1968. | 1362. | 1431. | 692. | 692. |
| 12 | 1220. | 1042. | 1376. | 1264. | 2100. | 1635. | 1250. | 843. | ¢22． | 469. |
| 13 | 423. | 881. | 625. | 817. | 725. | 1346. | 1030. | フ9ร． | 380. | 557. |
| 14 | 87. | 228. | 474. | 403. | 363. | 404. | 961. | 649. | 384. | 223. |
| TOTAL STLLK BIUMASS UN 1．JANLATY M |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
|  | 1028415． | 963736. | 895084. | 640121. | 546108. | 543408. | 588188. | 659283. | 770812. | 794713. |
| 57／476． |  | ON 1．Jinuair | FY CAGE AT | FIRSI MAT： | 5 264722 | 267546 | 251493 | 27\％165． | 279706 |  |
|  |  | － |  | $2 \mathrm{S4}$ ． |  |  | ， | 2ワッ165． | 27006． | 42.2124. |
|  |  |  |  |  |  |  |  |  |  | ＇Contimued |



BIOMASS OE GTHEK EGOD ASSUMED TO REMAIM CONSTANT







stock numbers Handock

| HGE | 19\%4 | 1975 | 1976 | $19 \% 7$ | 1.978 | 1979 | 1980 | 1981 | 1983 | 1983 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| , | 1,33342056. | E844534. | 6059245. | フ95398. | 16192032. | 25247356. | 7854985. | 14009270. | 14186492. | 16313359. |
| 1 | 11598661. | 14174903. | 1077205. | 1243861. | 2221221. | 3204233. | 521.6298. | 1290745. | 2242907. | 2100361. |
| 2 | 375934. | 1256142. | 2255660. | 190119. | 26043?. | 397050. | 765023. | 1298435. | 278272. | 469295. |
| 3 | 609538. | 92053. | 316795. | 657112. | 46548. | 64773. | 112648. | 267480. | 564690. | 123723. |
| $\stackrel{4}{4}$ | 94772. | 191317. | 20426. | 62019. | 182599. | 11652. | 16264. | 26818. | 87519. | 191513. |
| 5 | 4509. | 26901. | 46749. | 7054. | 13944. | 48027. | 2958. | 3955. | 3189. | 32681 . |
| $\bigcirc$ | 1546. | 1989. | 7964. | 10294. | 2174. | 3662. | 15006. | 774. | 1575. | 3804. |
| \% | $1663 \%$. | 911. | 782. | 2268. | 3096. | 726. | 1100. | 4973. | 329. | 704. |
| 8 | 1587. | 4217. | 214. | 474. | 847. | 837. | $37 \mathrm{s}$. | 366. | 1733. | 103. |
| 9 | 111. | 352. | 1126. | 115. | 285. | 350. | 284. | 196. | 187. | 579. |
| 10 | 69. | 71. | 62. | 311. | 73. | 134. | 166. | 71. | 101. | 134. |
| TOTHL STOCK RIGMASS ON 1. JANLJARY |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
|  | 22398.94. | 1500551. | 759373. | 516089. | 507183. | 634049. | 675443. | 613925. | 620404. | 586110. |
| 5 Fabl | 16 STOCK $\begin{gathered}\text { GIOM } \\ 371359 .\end{gathered}$ |  | ARY 621492 | EIRST MAT. 326991. | 2) 185334. | 150870. | 221319. | 380899. | 317029. | 271751. |



| FISH LNG MORTALITY |  |  | 1975 |  |  |  |  |  |  | 1981 | 1982 -1983 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| abe |  | 1974 |  | 1976 | 1977 | 1978 | 1979 |  |  |  |  |  |
| 0 |  | 0.1533 | 0.3442 | 0.3610 | 0.2396 | 0.0907. | 0.1187 |  | 0.1214 | 0.6623 | 1.0013 | 0.6071. |
| 1 |  | 0.6548 | 0.9955 | 0.4070 | 0.4923 | 0.3132 | $0 \times 1947$ |  | 0.0583 | 0.1296 | 0.1720 | 0.4253 |
| 2 |  | 0.9882 | 1.2306 | 1.3353 | 0.2324 | 0.0253 | 0.0910 |  | 0.1349 | 0.1230 | $0.1027=$ | 0.1505 |
| 3 |  | 0.8480 | 1. 4280 | 1.2024 | 1.4016 | 0.6437 | 0.0728 |  | 0.4108 | 0.1718 | 0.1844 | 0.1318 |
| 4 |  | 0.9120 | 1.3572 | 1.8248 | 0.3256 | 0.1106 | 0.1096 |  | 0.3716 | 0.3383 | 0.1453 | 0.1159 |
| 5 |  | 1.2266 | 1.3695 | 2.0351 | $1.7342^{*}$ | 0.0129 | $0.0598^{\circ}$ |  | 0.3422 | 0.6457 | 0.1893 | 0.1638 |
| 6 |  | 1.1230 | 1.4475 | 1.0424 | 2.0767 | 0.1596 | 0.0095 |  | 0.0774 | 0.6447 | 0.2747 | 0.4494 |
| 7 |  | 1. 1538 | 2.7291 | 3.9877 | 0.6914 | 0.4725 | 1.4474 |  | 0.0765 | 1.3079 | 0.4289 | 1.0719 |
| 3 |  | 1.3308 | 1.0837 | 1.1099 | 1.0082 | 0.20886 | 0.3371 |  | 0.4912 | 0.4343 | 0.7697 | 1.6120 |
| MEATH | E | WEIGHTEL EY | Stock Numbers | for the mature | Stock <AGE | AT EIIST | MAT. 3) |  |  |  |  |  |
|  |  | 0.2030 | 0.3137 | 0.3088 | 0.2694 | 0.0143 | 0.0204 |  | 0.0881 | 0.0707 | 0.0392 | 0.0334 |


FEEUATION MORTALITG HERRING

| nig | 1974 | 1975 | 1976 | 1977 | 1978 | 1979 | 1980 | 1981 | 1982 | 1983 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | 1.1833 | 4.0929 | 0.9231 | 0.9464 | 0.9146 | 0.8562 | 1.0488 |  |  |  |
| 1 | 0.4867 | 0.3586 | 0.4164 | 0.2884 | 0.3276 | 0.3472 | 0.3103 | 0.9488 0.3887 | 1.0043 0.3014 | 0.8263 0.3713 |
| 2 | 0.0421 | 0.0324 | 0.0294 | 0.0218 | 0.0235 | 0.0241 | 0.0223 | 0.0269 | 0.0258 | 0.0322 |
| 3 | 0.3111 | 0.3305 | 0.3206 | 0.2826 | 0.2967 | 0.3173 | 0.3058 | 0.3409 |  | 0.0322 |
| 4 | 0.0628 | 0.0414 | 0.0347 | 0.0202 | 0.0203 | 0.0199 | 0.0168 | 0.0216 | 0.3255 0.0198 | 0.3796 0.0369 |
| 5 | 0.1891 | 0.1251 | 0.1055 | 0.0628 | 0.0660 | 0.0634 | 0.0526 | 0.0696 | 0.0198 | 0.0369 |
| ; | 0.0002 | 0.0002 | 0.0002 | 0.0002 | 0.0002 | 0.0003 | 0.0002 | 0.0003 | 0.0620 | 0.1211 |
| 7 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0003 0.0000 | 0.0003 |
| e | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 0.0000 |
|  |  |  |  |  |  |  | . |  |  | fontimed |


| EISHING | g murtality | NORWAY FOUT |  |  |  |  |  |  |  | 1983 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Age | 1974 | 1975 | 1976 | 1977 | 1978 | $1979^{\circ}$ | 1980 | 1981 | 1982 |  |
| $\checkmark$ | 0.0392 | 0.0625 | 0.0495 | 0.0261 | 0.0120 | 0.0018 ： | 0.0079 | 0.2236 | 0.0072 | 0.2202 |
| 1 | 0.9586 | 0.8792 | 0.7581 | 0.6889. | 0.5416 | 0.5217 | 0.0797 | 0.2713 | 0.6033 | 0.66558 |
| 2 | 2.0159 | 0.7855 | 2.2257 | 0.7274 | 0.8744 | 1.1767 | 1.5834 | 0.0484 | 0.3772 | 1.4296 |
| 3 | 1．7623 | 0.5847 | 0.5437 | 0.9796 | 1.3729 | 0.9014 | 0.7892 | 1．3839 | 0.0227 | 0.4172 |
| MEAN E W | WElghted hy | STOCK NUMAERS | for the mature | Stock lage | At ETkSt | MAT． 15 |  |  |  |  |
|  | 0.1300 | 0.1435 | 0.1340 | 0.1462 | 0.1221 | 0.1129 | 0.0187 | 0.0273 | 0.0834 | 0.1100 |


| COCK numbers norway pout |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4 AE | 1974 | 1975 | 1976 | 1977 | 1978 | 1979 | 1980 | 1981 | 1982 | 1983 |
| 0 | 930970240. | 851525375. | 534479904. | 2498フォク76． | 432158656． | 3039867904. | 283406752. | 607993920. | $5 \overline{56503488 .}$ | 43912680. |
| 1 | 391510944. | 157219240． | 142543328． | 106474128. | 56886668. | 103549016. | 774175232. | 77968816. | 126052840． | 142996704． |
| 3 | 2743816． | 8806204. | 5446292. | 7317074. | 8720719. | 5014789. | 9428303. | 121353392. | 7906907. | 9913181. |
| 3 | 3142553. | 107357. | 1264951. | 515271. | 1271032. | 1214864. | 517604. | 656337. | 38340256. | 1995579. |
|  |  |  |  |  |  |  |  |  |  |  |
| $55^{\circ} \mathrm{H}$ UNEINT | ． 6955078. | 1724942． | 1568796. | 1179037. | 946763. | 2507330. | 6380709. | 4179624. | 3209097. | 1479718. |
|  | stuck biom | ASS DN 1．J | NuARY（age | EIRST MAT． | 1） |  |  |  |  |  |
|  | 3229592. | 1298179. | 1301556. | 1054099. | 730683. | 987396. | 6239006. | 3975637. | 2924805. | 1457762. |

## PREDATTUN MGRTALITY NORWAY POUT

| MİE | 19\％4 | 1975 | 2976 | 1977 | 1978 | 1979 | 1980 | 1981 | 1982 | 1983 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.8754 | 0.7249 | 0.5640 | 0.4539 | 0.4168 | 0.3660 | 0.3353 | 0.3341 | 0.3733 | 0.4450 |
| 1 | 1.8359 | 1.3475 | 1.1453 | 0.8133 | 0.8871 | 0.8747 | 0.7744 | 0.9646 | 0.9552 | 2.4749 |
| 2 | 0.2177 | 0.1549 | 0.1323 | 0.0891 | 0.0967 | 0.0942 | 0.0814 | 0.1038 | 0.0996 | 0.1713 |
| 3 | 2.1570 | 1.3443 | 1.1438 | 0.9085 | 1.2358 | 1.0559 | 0.9211 | 1.2569 | 1.2644 | 2.3548 |
|  | mass or | ER EOOD | mer IO | N CONSTA |  |  |  |  | ／Continued |  |


STOCK NUMBERS SPRAT

| AGE | 194 | 1975 | 1976 | 1977 | 1978 | 1979** | 1980 | 1981 | 1982 | 1993 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| , | 73433420.5. | 556014720. | 242462449. | 109574176. | 291960000. | 138671472. | 83592295. | 47660172. | 38816432. | 24703812. |
| 1 | 620699712. | 369312904. | 285060320. | 137323904. | 122813440 . | 177535296. | 82137240. | S1272184. | 32239780. | 28090622. |
| $\because$ | $37760 \% 68$. | 2035864.6. | 11680735: | 39198600. | 50703048. | 30508298. | 47379524. | 21362010. | 14060516. | 7840564. |
| 2 | 6r93935. | 10646629. | 14994168. | 15174110. | 10499755. | 5561363. | 2128781. | 2146703. | 日95684. | 949254* |
| 4 | 28591.3. | 2489771. | 1546034. | 1185736. | 6303181. | 1209595. | 703031. | 47029. | 141605. | 43242. |
|  |  |  |  |  |  |  |  |  |  |  |
| Spabintina | 4168011. | 4208915. | 2851134. | 1849744. | 1550205. | 1.349096. | 912511. | 501679. | 325167. | 237704. |
|  |  | ass on 1.1 | nuaky cage a | FIRST MAT. |  |  |  |  |  |  |
|  | 543446. | 1989348. | 1304501. | 1063337 | 790157. | 392084. | 450026. | 231438. | 14460. | 84899. |




## STOCK NUMEERS SANIEEL

| AgE | 1974 | 1975 | 1976 | 1977 | 1978 | 1979 | 1980 | 1981 | 1982 | 1983 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ' | 1421964928. | 932929726. | 848484234. | 726962112. | 520712512. | 529062592. | 290627584. | 531611232. | 72728520. | 46497884. |
| 1 | 162723296. | 2155\%9760. | 128\%31688. | 188127552. | 241306064. | 150925120. | 177824608. | 116406728. | 227770256. | 29868792. |
| 5 | 34722156. | 30205862. | 57931412. | 26664214. | 45400904. | 53107748. | 50087040. | 39101716. | 38386723. | 67093400 . |
| 3 | 6911630. | 10095706. | 6730407. | 12301499. | 7084221. | 9367872. | 91495\%4. | 10601697. | 7119861. | 14117784. |
| 4 | $703170 \%$. | 3336586. | 3520299. | 3190616. | 3310548. | 3215219. | 2306744. | 2210780. | 4899780. | 1785511. |
| 5 | 1064968. | 1763471. | 1077880. | 850939. | 1010486. | 1092476. | 836618. | 901272. | 541857. | 1442793. |
| 0 | 144i45. | 421337. | 506024. | 504060. | 165077. | 561345. | 349978. | 434149. | 291019. | 299716. |
| TUTAL STOCK gIOMASS ON i. JANUARY SOM. |  |  |  |  |  |  |  |  |  |  |
|  | 2662063. | 2476594. | 2210073. | 2145716. | 2360490. | 2091898. | 1934105. | 1713074. | 1888113. | 1260941. |
| 5 P AWN |  | ASS ON 1. . GA . | NUARY ${ }^{\text {SGGE }}$ 887627. | $\begin{aligned} & \text { EIKST MAT. } \\ & \text { G23508. } \end{aligned}$ | 2) 737390. | 874022. | 812480. | 705751. | 691079. | 1074399. |



Tahle 2．4．2．Comparison of different runs of the multispecies VPA． For each run on assumption changed compared to the＂Koy kun＂． Run 2：Half feeding level $+++*$ Run 3 ：Tntal hiomass conctant Run 4：＂Other fond＂disreqarded t＋＊＊kun b ：half M1 Run o：Suitability adjustment factor．
（For a more detailed description of the runs see sect 2．8．and 2．9）
species：COD


Fisuiny fortality
（1ean リy（y－ss）

| 13 | 9.100 | ＋ 11.00 | 0.310 | 0.611 | 0.110 | 0.01 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 7.19 | ＊ 17.27 | 0.19 | iJ． 19 | 11.31 | 1）．20： |
| 2 | 7.91 | ＊ 0.4 ？ | 0.41 | 7． 4.1 | 0.94 | 0.42 |
| 3 | 1.08 | ＋ 1.118 | 1.117 | 1．48 | 1.16 | 1.08 |
| 4 | 0.72 | ＊ 0.72 | 9.72 | 7.72 | 0.74 | 0.72 |
| 5 | 0.74 | ＋11．14 | 7.14 | 11.14 | 15.61 | 0.74 |
| 6 | 7.72 | ＊ 0.72 | ก． 3 ？ | 7． 12 | 1.73 | 0.72 |
| 7 | 1.71 | ＋ 0.77 | 11.11 | 1）． 17 | 11.34 | 0.77 |
| $x$ | 9.77 | ＊7． 77 | ก． 17 | 0.70 | 0.84 | 1 6.77 |
| $y$ | 0.87 | ＋1）．37 | 1.81 | $11.0 \%$ | 0.95 | 0.87 |
| 10 | 7.80 | ＊$\quad .80$ | 2． 380 | 11.80 | ก． 57 | 0.30 |

－Predation riortality（iean $1 y(y-\sigma .5)$

| 17 | 1.46 | ＋ 0.26 | 1．10？ | 1，4i | U．44 | 10.10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 7.21 | －！．10 | 11.29 | 0.80 | リ．21 | 1：0．1） |
| ？ | 7.027 | ＊ 0.013 | ก．133．2 | 11．02．${ }^{\text {a }}$ | 1）． $22 \%$ | 0.012 |
| $s$ | 1.1011 | ＋0．006\％ | 11.111 b | 1）． 1111 | 1．111 | $0.1103 \%$ |
| 4 | 9．0\％ | ＊ 3.01 n | ก． 110 | 0.60 | 0．0．0 | 0.00 |
| $b$ | 9．［．1） | ＋ 11.10 | （1．00 | U．U11 | 0．nil | 0.010 |
| \％ | ）． 00 | ＋ 0.00 | 0.107 | ）．0n | 10．7） | 0.110 |
| 1 | リ．fill | ＋ 9.1111 | 7． 1111 | 0.000 | 10.010 | 11.119 |
| ＊ | 9.10 | ＊ 7.110 | 9.00 | 17.00 | i．${ }^{\text {an }}$ | 0.00 |
| 9 | 1）． 1111 | ＋ 0.00 | ก．00 | 11.011 | （1）．11） | U． 011 |
| 10 | n． 0 n | ＊ 0.00 | ก． 7 | 1.00 | 0．0．7 | 0.010 |
| － | $k$ in nu | unhers | （ Mean ly | －is）（trin | sands） |  |
| $1)$ | ？ 311570 | $+249753$ | susbuy | 2004402 | 25：3149 | 2．514 3 |
| 1 | 197701） | ＋ 144318 | 200131 | 1976） | 174249 | 1446／4 |
| ？ | 36.312 | ＊ 35758 | ．30727 | 8030\％ | 30893 | あら×2ら |
| 3 | 23651 | ＋ 23639 | ？ 30611 | 23631 | 71034 | 23645 |
| 4 | 7557 | 7950 | 7957 | 79力7 | 7343 | 7950 |
| 5 | 2390 | ＋ 2393 | 2390 | 2．34\％ | 2601 | 2．84\％ |
| 6 | 1104 | ＋ 1174 | 1104 | 1114 | 1321 | 1104 |
| 7 | 411 | ＋ 411 | 411 | 411 | 302 | 411 |
| $\stackrel{\rightharpoonup}{*}$ | 152 | ＋15？ | 152 | 152 | 128 | 132 |
| $y$ | 75 | ＋ 75 | 73 | 13 | 68 | 13 |
| 1 r | 51 | ＋ 51 | 31 | b1 | 47 | 1 |

／Continued

## Table 2.9.1. (Continued)

Comnarison of different runs of the fultiapecies Vra. Frr each run, one assumption nas been changed compared to the key run. Run 2: Half feering lovel *** Kun 5 : Total hiomass constant kun 4: "Dtner fond" disrenarded *+t* kun 5 :italf M1 Qill ó: cuitability adjustment factor.
(For a more detailed description nf the runs see sect z̈. 8 and 2.9)
sracies: VHITING


| 17 | 11.03 | * 0.32 | 10. 34 | 1.71 | U.86 | 0.23 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1).58 | * 0.33 | 1. 38 | 11.87 | 0.61 | 0.34 |
| $?$ | 0.19 | * 0.10 | 0.19 | 1.27 | 0.20 | 0.16 |
| 3 | 0.11 | + 0.00 | 0.11 | 0.13 | U. 11 | 0.10 |
| 4 | ก.0\% | + 0.04 | 7. 09 | 1).13 | 0.08 | 0.04 |
| $b$ | 0.15 | + 0.02 | 0.135 | U. 06 | 0.114 | 0.114 |
| 6 | 0.15 | * 7.02 | 7.03 | 0.05 | 0.05 | 0.93 |
| 7 | 0.05 | + 0.00 | 0.017 | 0.110 | $0.01)$ | 0.00 |
| 8 | 0.10 | * 0.00 i | $0.0 \%$ | 7.00 | 0.00 | 0.00 |
| 9 | 19.100 | * 0.010 | 7. 1100 | 10. 110 | 0.011 | 1.0011 |
| 10 | 9. ${ }^{\text {a }}$ ( | * 0.00 | 0.100 | 0.10 | 0.07 | 0.00 |
| -- | cte in nt | umbers | (Mean 197 | -53) (tn | ลnกs) |  |
| $1)$ | 52.01170 | + 2300774i | 31 y9277 | 5998314 5 | 2.099090 | 2095334 |
| 1 | 2865? 28 | + 5727961 | 97:61326 | 1i)6?085 | $86 ? 274$ | 459010 |
| 2 | -58920 | + 3038281 | 538483 | 564070 | 483547 | 331805 |
| 3 | 2. 51415 | + 2214621 | 231193 | 238812 | 212.638 | 229252 |
| 4 | 86.032 | + 345021 | 36010 | 87131 | 87898 | 85634 |
| 5 | 21761 | + 21597 | 21759 | 21872 | ? 1088 ? | 21690 |
| is | 434:7 | - 4370i | 4539 | 4550 | 4099 | 433' |
| 7 | 1749 | + 1779 | 1049 | 1049 | 486 | 1049 |
| * | 263 | + 265 | 265 | 265 | 246 | 203 |
| 4 |  | + 64 | 04 | 64 | 59 | 04 |
| 10 | 10 | + 161 | 10 | 16 | 15 | 10 |

## Table 2.9.1. (Continued)

Comparison of different runs of the inultiapecies vpa. For each run, one assumption has been changed compared to the key run. qun ?: talf feeding level $\downarrow+\ldots \neq$ Run $s:$ Total hiomass constant Run 4: "Otner finad" disremarded $+*+t$ Run b :Half 171 qun 6: suitability adjustment factor.
(For a more fetailed description of the runs see sect 2.8 and 2.9)
species: FADOnck


- stock in numbers (lean 1919-ல3) (tmnusands)

| d | 3980373 | + 3525197 | 5019151 | 11176194 | 4304743 | 3654003 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| , | 770318 | + 6939631 | 770031 | ல55274 | 056330 | 149940 |
| ? | 2 5 こ541 | + 2863111 | 243352 | 246190 | 263540 | 293604 |
| $\leq$ | 951710 | + 413461 | 931970 | 43030 | 36714 | 43805 |
| 4 | 24350 | + 243031 | 24361 | 243:8 | 23265 | 24431 |
| , | 80.70 | + 8074i | 3076 | 8070 | 7530 | 8075 |
| 6 | 2154 | + $2154 i$ | 2154 | 2154 | 1972 | 2154 |
| 7 | 705 | + 7133 | 703 | 7115 | 635 | 7105 |
| $\underset{\sim}{x}$ | 322 | + 32? | 322 | 322 | 293 | 322 |
| 9 | 154 | * 159 | 159 | 159 | 147 | 159 |
| 10 | 5.3 | + 58 i | 58 | 53 | 53 | ל8 |

/Continued

Table 2.9.1. (Continued)

Comnarison of different runs of the ultiapecips VPA. For each run. one assumption has been chancied compared to the key run. wun 2: Half foedinc level $+++\downarrow$ Run 5 : Total biomass constant Run 4: "'sther fond" disrefarded t+** kun b :Half MT Run 6: Suitability arjustinent factor. (For a more fotailed description $n$ the runs see sect 2.8 and 2.9)
sfecies: HERRING


Comparison of different runs of the fultisfecies VrA. For each run, one ascumption has been chanded compared to the rey run. Run 2: :alf feeding level $+*+4$ Run 3: Total binmass corstant Run 4: "other food" diaregarder! +4*+ tiun b :Half M1 Run $6:$ suitability adjustment factor.
(For a nore detailed deacription of the runs see sect z. 8 and 2.9) spocies: Sprit


Spiecies: Pokway pout
Are i Key izun * Run ? i kun 3 i kun 4 i kun 5 i kun 0 i


Table 2.9.1. (Continued)

Comnarison of difterent runs of the multirpecies VPA. Fer each run, one assumption has been chanced compared to the key run. Run ?: Half feerling level $++4 *$ Run 3: Total hinmasa constant Run 4: "other fond" disrogarded **** Run 5 :Half M1 Run 6: Suitahility afjustment factor.
(for a more detailed description $n f$ the runs see sect 2.8 and 2.9)
sfecies: salmeel.


Table 2.9.2 Changes compared to Key run

| SPECIES | $\frac{\text { RUN } 2}{\text { Feeding level }} \begin{aligned} & 0.5 \end{aligned}$ |  |  | RUN 3 <br> Total biomass constant |  |  | $\begin{gathered} \text { RUN } 4 \\ \hline \text { "Other food" } \\ \text { ignored } \end{gathered}$ |  |  | $\frac{\text { RTN } 5 .}{\frac{\text { MI }}{\text { halved }}}$ |  |  | $\frac{\text { RUN } 6}{\substack{\text { Suitability } \\ \text { ad,justed }}}$ |  |  | COMMENTS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | F | N | M2 | F | N | M2 | F | N | M2 | F | N | M2 | F | IV | M2 |  |
| COD | 100 | 94 | 49 | 100 | 100 | 100 | 94 | 104 | 139 | 109 | 88 | 103 | 100 | 92 | 30 | Age groups 1 - 3 |
| WHITIING | 104 | 68 | 57 | 100 | 100 | 100 | 97 | 2993 | 159 | 113 | 85 | 102 | 100 | 62 | 54 | Age groups 0-5 |
| SAITHE | - | - | - | - | - | - | - | - | - | ? | ? | ? | - | - | - |  |
| MACKEREL | - | - | - | - | - | - | - | - | - | ? | ? | ? | - | - | - | - - - |
| HADDOCK | 104 | 56 | 65 | 100 | 100 | 100 | 97 | 279 | 158 | 109 | 85 | 101 | 100 | 66 | 79 | Age groups 0-5 |
| HERRING | 105 | 67 | 54 | 100 | 99 | 100 | 91 | $186^{\text {T }}$ | 151 | 107 | 92 | 95 | 102 | $244{ }^{\text {x/xta }}$ | 96 | Age groups 0-6 |
| SPRAT | 120 | 58 | 54 | 100 | 100 | 100 | 86 | 226 | 149 | 104 | 88 | 96 | 103 | 123 | 104 | Age groups 0-4 |
| N. POUT | 116 | 55 | 65 | 100 | 102 | 100 | 90 | 269 | 174 | 129 | 37 | 111 | 100 | 155 | 100 | Age groups 0-4 |
| SANDEEEL | 116 | 64 | 58 | 100 | 101 | 100 | 82 | 485 | 200 | 85 | 88 | 81 | 68 | 99 | 78 | Age groups 0-5 |

Run 1: Key run - No adjustment
Helgason-Gislason other food model VIl as in Fish Stock Assess. Working Group Feeding level = I
In each subsequent run only one assumption changed
Fi) O-group 1983 extremely high
(\#)
Abnormal Y.C. (not raised run)

Table 3.3.1 Fxtreme values of predation mortality for the 3 youngest ages of each species (excluding SATTHE and MACKERHU) together with upset $=\exp \{(\mathrm{M} 2($ high $)-$ M2 $($ low $)) / 2\}$

| $\qquad$ | 0-Group |  |  | 1-Group |  |  | 2-Group |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | M2 (Low) | M2(High) | UPSET | M2(Low) | M2 (High) | UPSEP | M2 (Low) | M2 (High) | UPSEI |
| Cod. | . 37 | . 52 | 1.08 | . 16 | . 30 | 1.07 | . 02 | . 05 | 1.02 |
| Whiting | . 80 | 1.06 | 1.14 | . 40 | . 69 | 1.16 | . 16 | . 31 | 1.08 |
| Haddock | 1.24 | 1.77 | 1.30 | . 84 | 1.55 | 1.43 | . 15 | . 27 | 1.06 |
| Herring | . 84 | 1.21 | 1.20 | . 29 | . 49 | 1.11 | . 02 | . 04 | 1.01 |
| Sprat | . 21 | . 57 | 1.20 | . 52 | . 97 | 1.19 | 1.14 | 1.95 | 1.50 |
| Norway Pout | . 33 | . 88 | 1.32 | . 77 | 1.84 | 1.71 | . 08 | . 22 | 1.07 |
| Sandeel | . 43 | 1.73 | 1.92 | . 43 | 1.02 | 1.34 | . 40 | . 84 | 1.22 |

Table 4.3.1 Estimated state of fish stocks at steady-state under current levels of fishing mortality


Table 4.3.2 Estinated steady-state yield in each fishery ( 1000 tonnes) in each fishery at current levels of fishing mortality.

| Fishery | Cod | Whiting | Saithe | Mackerel | Haddock | Herring | Sprat | Norway Pout | Sandeel |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Roundfish <br> (human consumption) |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \text { Demersal } \\ & \text { (Industrial) } \end{aligned}$ |  |  |  |  |  |  |  |  |  |
| Pelagic <br> (Industrial) |  |  |  |  |  |  |  |  |  |
| Herring (human consumption) |  |  |  |  |  |  |  |  |  |
| Saithe |  |  |  |  |  |  |  |  |  |
| Mackerel |  |  |  |  |  |  |  |  |  |

Table 4.3.3 Expected change of steady-state biomass ${ }^{\text {FF }}$ ( 1000 t ) resulting from a $10 \%$ increase of $F$ in each fishery.

| Fishery in which Fis increased | Cod | Whiting | Saithe | Mackerel | Haddock | Herring | Sprat | Norway Pout | Sandeel |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Roundfish (human consumption) |  |  |  |  |  |  |  |  |  |
| Demersal <br> (Industry) |  |  |  |  |  |  |  |  |  |
| Pelagic (Industry) |  |  |  |  |  |  |  |  |  |
| Herring (Human consumption |  |  |  |  |  |  |  |  |  |
| Saithe <br> Mackerel |  |  |  |  |  |  |  |  |  |

F Together with similar tables for total yielid and recruitment

Mabla 4.3.4 Estinated change of steady-stata yielid ( 000 t ) in each fishery resulting from a $10 \%$ increase of $F$ in each fishery. Fishery = Roundfish (Humain consumption) ${ }^{\text {\#ت }}$

${ }^{\text {F }}$ Together with similar tables for all other fisheries

Table 6.1.1. Comparison of estimated weights (in '000 tonnes) consumed by North Sea COD of various exploited fish species in the years 1967 to 1970 (Daan, 1973) with values obtained using similar procedures for 1981

| Species | Average $1967 / 1970$ | 1981 |
| :--- | :---: | :---: |
| Cod | 56 | 38 |
| Haddock | 134 | 112 |
| Whiting | 47 | 98 |
| Norway pout | not available | 101 |
| Herring | 57 | 50 |
| Sprat | not available | 41 |
| Sandeels | not available | 131 |
| Plaice | 17 | 3 |
| Sole | 7 | 2 |
| Mackerel | 41 | 22 |

Table 6.1.2. Comparison of feeding coefficients for $\operatorname{COD}\left(\varnothing=L^{3} /\right.$ s) where I represents the average length and $S$ represents average stomach content weights obtained using various sampling programs (from Daan, 1983).

| Period | Area | Ø-value |
| :--- | :--- | :--- |
| $1966-1972$ | Total North Sea | .000158 |
| 1980 | Roundfish area 6 | .000147 |
| 1981 | Total North Sea | .000151 |
|  | Average | .000152 |

Table 6.2.1 Comparison of Total consumption in tonnes by individual predators with estimated stock biomasses of prey in 1974 and 1981.

Predation Summary Table for the (Total) Year 1974

| PREY | PREDATORS |  |  |  | TOTAL | $\begin{gathered} \text { SIOCK } \\ \text { BIOMASS } \end{gathered}$ | $\begin{gathered} \% \\ \text { CONSUMED } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | COD | WHITING | SAITHE | MACKHREEL |  |  |  |
| Cod | 14143.5 | 695.1 | . 718.2 | 220.2 | 15777.8 | 395922 | 3.6 |
| Whiting | 87729.1 | 43030.5 | 3472.9 | 406.7 | 134639.4 | 862561 | 15.6 |
| Saithe | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 1028415 | - |
| Mackerel | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 1147761 | - |
| Haddock | 188849.4 | 154544.9 | 341288.2 | 28243.7 | 712926.2 | 2239894 | 31.8 |
| Herring | 21634.1 | 21022.7 | 5553.5 | 4629.5 | 52839.9 | 486618 | 10.9 |
| Sprat | 112124.0 | 425022.9 | 5726.4 | 209858.7 | 752732.1 | 4168011 | 18.1 |
| Norway Pout | 81239.6 | 90287.0 | 577533.9 | 281 071.7 | 1030132.3 | 3695078 | 27.9 |
| Sandeel | 64256.1 | 243660.4 | 17416.8 | 705537.8 | 1030871.1 | 2662063 | 38.7 |
| TOTAL | 569975.9 | 978263.7 | 951710.1 | 1229969.0 | 3729918.8 | 16686323 |  |

Predation Summary Table for the (Total) Year 1981

| Cod | 34252.3 | 2036.4 | 1 004.3 | 35.5 | 37328.5 | 505363 | 7.4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Whiting | 87042.6 | 34884.0 | 1780.8 | 11.8 | 123719.1 | 571206 | 21.7 |
| Saithe | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 659283 | - |
| Mackerel | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 191401 | - |
| Haddock | 90048.1 | 85931.9 | 45734.7 | 450.0 | 222164.7 | 613925 | 36.0 |
| Herring | 41264.5 | 114472.0 | 6570.5 | 1650.2 | 163957.2 | 651375 | 25.2 |
| Sprat | 48234.5 | 119885.9 | 538.2 | 3084.3 | 171742.9 | 501679 | 34.2 |
| Norway Pout | 81463.9 | 145031.2 | 287377.0 | 46487.5 | 560359.6 | 4179634 | 11.7 |
| Sandeel | 121856.1 | 273832.4 | 9779.4 | 84945.6 | 490413.6 | 1713074 | 27.2 |
| TOTAL | 504162.0 | 776073.9 | 352784.9 | 136664.9 | 1769685.8 | 9586940 |  |

[^1]Table 6.2.2 Environnental impact statement in respect of predation exercised by various predator species in the North Sea on HADDOCK.

PARTITAL PREDAATION MORTMASITIES

| Haddock | M2 | COD |  |  |  |  |  | WHITING |  |  |  |  |  | SAITHE |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 | 5 | $6+$ | 1 | 2 | 3 | 4 | 5 | $6+$ | 4 | 5 | 6 |
| Age 0 | 1.4197 | . 0076 | . 1696 | . 0456 | . 0207 | . 0058 | . 0011 | . 016 | . 345 | . 293 | . 080 | . 02 | . 014 | . 0196 | . 167 | . 204 |
| 1 | 1.0376 | . 0052 | . 1881 | . 1902 | . 1180 | . 0480 | . 0268 | . 016 | . 019 | . 056 | . 026 | . 007 | . 006 | . 033 | . 144 | . 170 |
| 2 | . 1567 |  | . 0051 | . 0348 | . 0531 | . 0314 | . 0275 |  | . 00009 | . 0016 | . 0008 | . 0002 | . 0002 | . 0002 | . 0006 | . 001 |
| 3 | . 0424 |  | . 0005 | . 0022 | . 0080 | . 0057 | . 0260 |  |  |  |  |  |  |  |  |  |
| 4 | . 0375 |  | . 0001 | . 0018 | . 0026 | . 0013 | . 0317 |  |  |  |  |  |  |  |  |  |
| 5 | . 0146 |  |  |  | . 0005 |  | . 0141 |  |  |  |  |  |  |  |  |  |

INDIVIDUAL PREDATION MORTIALITIES $\times 10^{9}$

| 0 | . 037 | . 54 | . 97 | 1.3 | . 7 | . 3 | . 01 | . 2 | . 5 | . 4 | . 5 | . 7 | . 35 | 3.0 | 4.8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | . 025 | . 60 | 4.1 | 7.5 | 6.2 | 5.4 | . 0099 | . 013 | . 09 | . 16 | . 20 | . 3 | . 58 | 3.0 | 4.0 |
| 2 |  | . 016 | . 74 | 3.4 | 4.0 | 8.8 |  | . 00006 | . 0028 | . 0020 | . 0051 | . 013 | . 0038 | . 013 | . 024 |
| 3 |  | . 002 | . 048 | . 51 | . 73 | 8.3 |  |  |  |  |  |  |  |  |  |
| 4 |  | . 000 | . 038 | . 17 | . 17 | 10.1 |  |  |  |  |  |  |  |  |  |
| 5 |  |  |  | . 030 |  | 4.5 |  |  |  |  |  |  |  |  |  |

Table 6.4.1. Andersen and Ursin Model versus the "Key Run"
Predation mortalities per year by species and age group in 1976
KR: Key Run AU: Andersen and Ursin

| Age | Cod |  | Whiting |  | Saithe |  | Mackerel |  | Haddock |  | Herring |  | Sprat |  | Sandeel |  | Norway Pout |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | KR | AU | KR | AU | KR | AU | KR | AU | KR | AU | KR | AU | KR | AU | KR | AU | KR | AU |
| 0 | 0.4 | 1.5 | 0.8 | 0.9 | 0 | 1.9 | 0 | 0.5 | 1.3 | 1.0 | 0.9 | 1.1 | 0.4 | 0.8 | 1.3 | 1.6 | 0.6 | 1.8 |
| 1 | 0.2 | 0.4 | 0.5 | 0.7 | 0 | 0.5 | 0 | 0.2 | 1.0 | 0.8 | 0.4 | 0.3 | 0.8 | 0.5 | 0.9 | 0.7 | 1.1 | 0.9 |
| 2 | 0.03 | 0.03 | 0.2 | 0.4 | 0 | 0.1 | 0 | 0.07 | 0.2 | 0.3 | 0.03 | 0.1 | 1.6 | 0.3 | 0.7 | 0.5 | 0.1 | 0.7 |
| 3 | 0.01 | 0.005 | 0.1 | 0.2 | 0 | 0.04 | 0 | 0.04 | 0.09 | 0.1 | 0.3 |  | 0.8 | 0.3 | 0.2 | 0.4 | 1.1 |  |
| 4 | 0 | 0 | 0.1 | 0.1 | 0 |  | 0 |  | 0.1 |  | 0.03 | 0.1 | 1.4 | , | 0.09 |  |  |  |
| 5 | 0 | 0 | 0.05 | $\} 0.07$ | 0 | \} 0.01 | 0 | \} 0.04 | 0.04 | \} 0.07 | 0.1 |  |  |  | 0.6 | 0.3 |  |  |
| 6 | 0 | 0 | 0.04 |  | 0 |  | 0 |  |  |  |  | ) |  |  | 0.9 |  |  |  |

Notes: AU exercise was done in January 1980. (JnpubI.)
O-Group: A\&U count from hatching .
KR counts from a later age (after metamorphosis)
Saithe: KR excludes young saithe from the North Sea; AU admit them.
Mackerel: KR has zero: material not ready.
Decrease with age: AU is smoother because food preference functions were used.
Ration: KR uses digestion rates as estimated from experiments.
AD calculated requixements from the growth equation (of. Section 2.1.4).

Table 6.6.1 Example of Uniqueness
Table for $f_{1}$ and $f_{2}$

| $f_{1}$ |  |
| :---: | :---: |
| $\overline{\mathrm{~N}}_{1}$ | $\overline{\mathbb{N}}_{2}$ |
| 800 | -147.27 |
| 820 | .107 .73 |
| 540 | -67.53 |
| 860 | -26.70 |
| 880 | 14.75 |
| 900 | 56.81 |
| 920 | 99.46 |
| 940 | 142.69 |
| 960 | 186.49 |
|  |  |
| $f_{2}$ |  |
| $\overline{\mathbb{N}}_{1}$ | $\overline{\mathbb{N}}_{2}$ |
| -95.97 | 22.00 |
| 483.57 | 27.00 |
| 409.38 | 32.00 |
| 1241.64 | 34.00 |
| 1512.42 | 42.00 |

Table 6.8.1 Estimated regression coefficients of $\ln$ ( $W$ (prey in stomach)/W(prey stock)) vs. In (Weight (predator)/W (prey stock)) for COD and WHITING preying on seven prey species, by calendar quarter.

| Parameter |  | $Q_{2}$ | $\frac{0 D}{23}$ | $\begin{array}{r} P \\ Q_{4} \quad \\ \hline \end{array}$ | E D A <br> $\Sigma Q$ | $Q_{1}$ | $\frac{W H}{Q_{2}}$ | $\frac{T I N}{G_{3}}$ | $Q_{4}$ | $\Sigma Q$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\alpha$ | -1.34 | -1.84 | -0.70 | -1.30 | $-1.33$ | -0.94 | -2.74 | -1.93 | -2.03 | -1.80 |
| $\beta$ | 0.25 | 0.33 | 0.15 | 0.29 | 0.26 | 0.03 | 0.59 | 0.47 | 0.48 | 0.34 |
| $v^{2}$ | 0.41 | 0.27 | 0.13 | 0.36 | 0.27 | 0.002 | 0.28 | 0.28 | 0.35 | 0.16 |
| $\hat{\eta}$ | -5.36 | -5.58 | -4.67 | -4.48 | -5.12 | -31.33 | -4.64 | -4.11 | -4.23 | -5.29 |
| $\begin{aligned} \text { H०: } & \text { Slopes } \\ & =0 \end{aligned}$ | 179.66 ㅍㅜㅢ |  |  |  |  | 56.18 \% ${ }^{\text {F }}$ |  |  |  |  |
| Ho: Slopes are $=$ | 3.93 ¥ 3 现 |  |  |  |  | 10.67 \# |  |  |  |  |
| Ho: Adjusted means = | 6.55 \# $x$ |  |  |  |  | 3.02 ¥ |  |  |  |  |

A) Prey species are: cod, haddock, whiting, Norway pout, herring, sprat, sandeel.
B) All age groups of all prey are included.

Table 6.8.2 Estimated regression coefficients of $\ln$ (W (prey in stomach) /W (prey in stock)) vs. In (Weight (predator) $W$ (prey in stock)) for COD and WHITING preying on seven prey species.

|  | Prey Species | $\alpha$ | Regression Coeff. |  |  | $\begin{gathered} \text { Ho: } \\ \text { Slopes }=\varnothing \end{gathered}$ | Но: Slopes = | $\begin{aligned} & \text { Ho: } \\ & \text { A.M. 'S }= \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Predator |  |  | $\beta$ | $>^{3}$ | $\hat{\eta}$ |  |  |  |
| COD | Cod | -1.14 | -0.24 | 0.07 | -4.75 |  |  |  |
|  | Haddock | -1.01 | 0.10 | 0.07 | -10.10 |  |  |  |
|  | Whiting | -0.50 | 0.05 | 0.01 | -10.00 |  |  |  |
|  | Norway Pout | -0.35 | 0.13 | 0.16 | -2.69 | 19.52 \#\# $\#$ | 8.57 ¥ $¥$ | 21.73 F |
|  | Herring | -1.84 | 0.45 | 0.28 | -4.09 |  |  |  |
|  | Sprat | -1.32 | 0.30 | 0.27 | -4.40 |  |  |  |
|  | Sandeel | -0.08 | 0.00 | $<0.01$ | - |  |  |  |
|  | All | -1.33 | 0.26 | 0.27 | -5.12 |  |  |  |
| WHITIING | cod | $-3.48$ | -0.85 | 0.35 | -4.09 |  |  |  |
|  | Haddock | -2.13 | 0.37 | 0.20 | -5.26 |  |  |  |
|  | Whiting | -0.95 | -0.43 | 0.23 | 2.21 |  |  |  |
|  | Norway Pout | 0.34 | -0.31 | 0.26 | -1.10 | 0.17 n.s. | 14.14 \#F | 39.35 \% |
|  | Herring | -4.00 | 1.04 | 0.27 | -3.85 |  |  |  |
|  | Sprat | -0.96 | 0.23 | 0.22 | -4.17 |  |  |  |
|  | Sandeel | 0.34 | -0.23 | 0.12 | -1.48 |  |  |  |
|  | All | -1.80 | 0.35 | 0.16 | -5.14 |  |  |  |

A) All age groups of prey included.


Figure 2.7.1. Plot of FF (ln $W$ (prey in stomachs)/W(prey in stock)) vs, ratio: (ln $W$ (predator)/W(prey in stock)) for various prey species eaten by cod.


Figure 2.7.2. Plot of FF (ln W (prey in stomachs)/W(prey in stock) vs. ratio (ln $W$ (predator) $/ W$ (prey in stock)) for various prey species eaten by whiting.







(



Figure 3.2.1. Reletionship of multispecies VPA estimates of l-year-old COD, Assessment Working Group VPA estimates of one-year-old cod and IYFS eatimates.



Figure 3.2.2. Relationship of multispecies VPA estimates of l-year-old HADDOCK, Assessment Working Group VPA estimates of one-year-old haddock and IYFS estimates.




Figure 3.2.3. Relationship of multispecies VPA estimates of l-year-old WHITING, Assessment Working Group VPA estimates of one-yearold whiting and IYFS estimates.




Figure 3.2.4. Relationship of multispecies VPA estimates of l-year-old HRRRING, Assessment Working Group VPA estimates of one-yearold herring and IYFS estimates.



Figure 3.2.5. Relationship of multispecies VPA estimates of l-year-old SPRAT, Assessment Working Group VPA estimates of one-yearold sprat and IYFS estimates.



Abnormal years excluded from regression

Figure 3.2.6. Relationship of multispecies VPA estimates of 1-year-old SANDEEL and Assessment Working Group VPA estimates of one-year-old sandeel made by summing the northern and southerm sandeel stocks.



Figure 6.8.1. Illustration of Equation 6.8.4. (Note that length groups are converted into weight groups.)

Rel. freq. and suitability



[^0]:    x) General Secretary ICES
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[^1]:    ZPURGE-I-NOFILPURG $=$ No files purged for DUAI: (PER.MS)

